The humanoid robot motion planning problem

Karim Bouyarmane

What I will talk about

- The path planning problem
 - Some algorithms
- The robot motion planning problem as a path planning problem
 - Some more algorithms
- The humanoid robot motion planning problem as a multi-modal (path/motion planning) problem
 - An algorithm
- The humanoid robot control problem
 - A universal controller

The path planning problem

How to go from point A to point B?

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 - get a map (download it)
 - encode relevant information your map (paths) in a graph-like structure (roadmap)
 - run your favorite graph search algorithm (Dijkstra, best-first, A*, D*, etc)
 - done

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 - Let's call this the "Google maps meta-algorithm"

How to go from point A to point B?

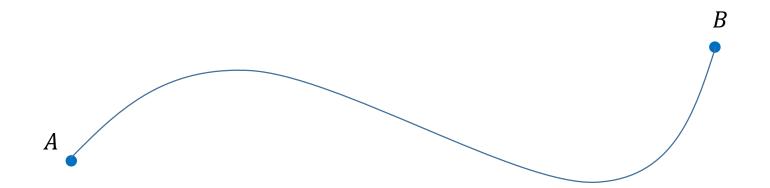
• Can we generalize the problem in a sound mathematical formulation?

- How to go from point A to point B?
 - What is "go"?
 - what are "points" A and B?
 - "what" needs to go (subject of the verb)?

- How to go from point A to point B?
 - What is "go"? → (Google maps) a path along the map
 - what are "points" A and B? → (Google maps) 2D points in the map
 - "what" needs to go (subject of the verb)? → (Google maps) a 2D point constrained to move along the edges of the graph

- Let's consider that the subject of the motion is a "point". Points are in the ideal mathematical sense, elements of a set, not in the physical point mass sense: no volume, no mass, no physics.
- how to make a point "move" from point A to point B in some set endowed with a notion of "continuity" and a notion of "path" ⇒ necessity of operating in a topological *space*
- The notion of motion is therefore associated with the notion of continuity and of topology

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- Answer: property of connectedness of the space?
 - Definition: a space is connected if it cannot be written as a union of two disjoint open sets/two disjoint closed sets

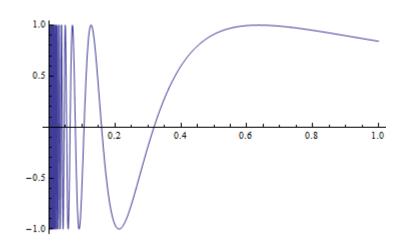
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- path-connected ⇒ connected, converse not true in general
 - counter example : the topologist's sine curve

$$\left\{ (x,y) \mid x = 0 \text{ or } y = \sin\left(\frac{1}{x}\right) \right\}$$

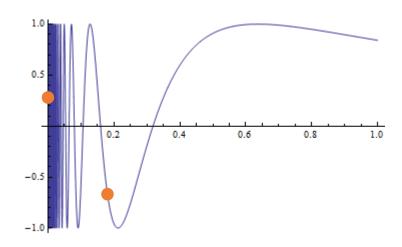
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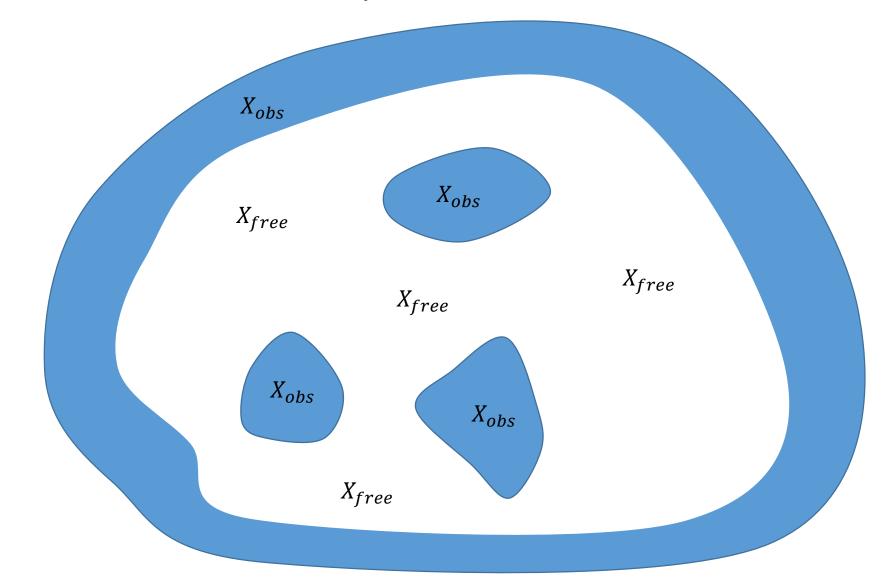
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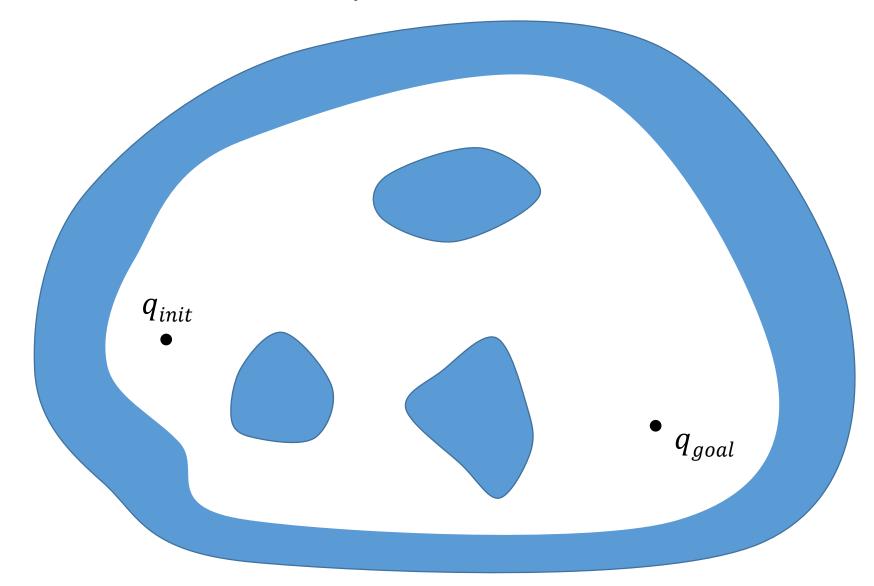


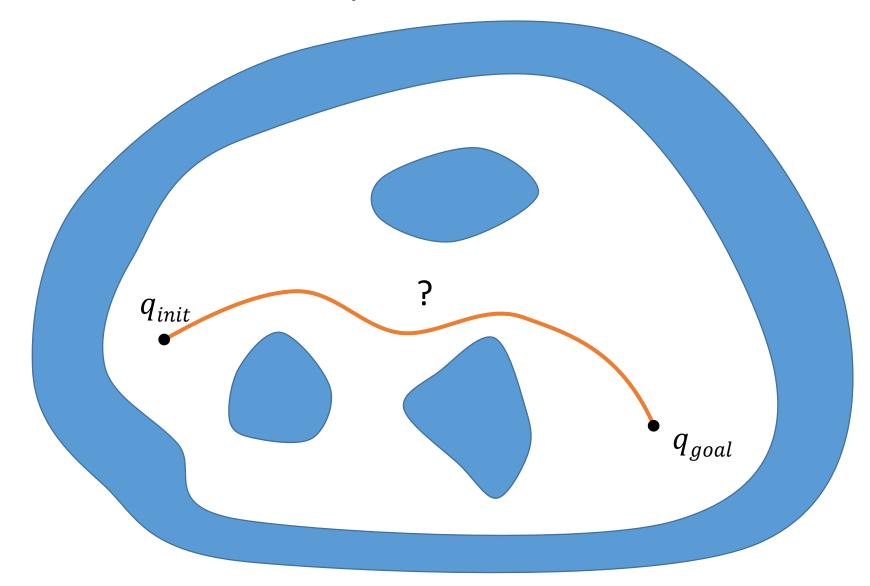
- For convenience, we will consider additional structure on our space X:X is a manifold of fixed dimension n (subset of \mathbb{R}^m locally homeomorphic in each of its points to \mathbb{R}^n)
- In this case: connected ⇔ path-connected
- Additional interesting properties worth studying in our context for the space X:
 - simply connected or multiply connected
 - Homotopy classes of paths (can a path be continuously deformed into another path)?
 - Fundamental group (How many topologically different (non homotopic) ways to go from a point to another)

Obstacles and Free Space

- Obstacles are compact subsets of $X: X_{obs}$
- The space X will be partitioned in two sub sets: $X = X_{obs} \cup X_{free}$
- Path planning algorithms will operate in X_{free} , avoiding X_{obs}
- X_{free} is an open set \Rightarrow no "optimal" path in general, we are not allowed to "touch" the obstacles





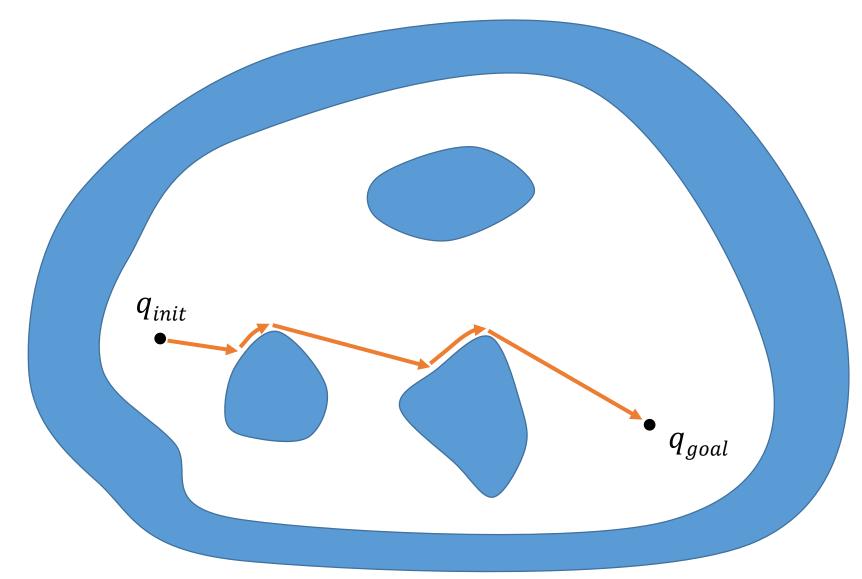


First algorithms

First algorithms

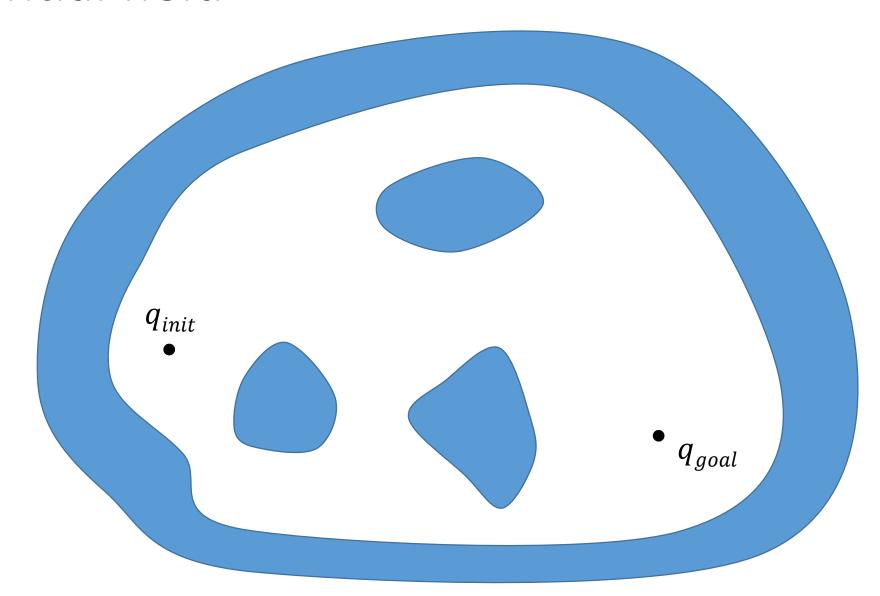
- Intuitive ideas:
 - The bug algorithm
 - Potential fields
 - Potential fields with occasional random walks

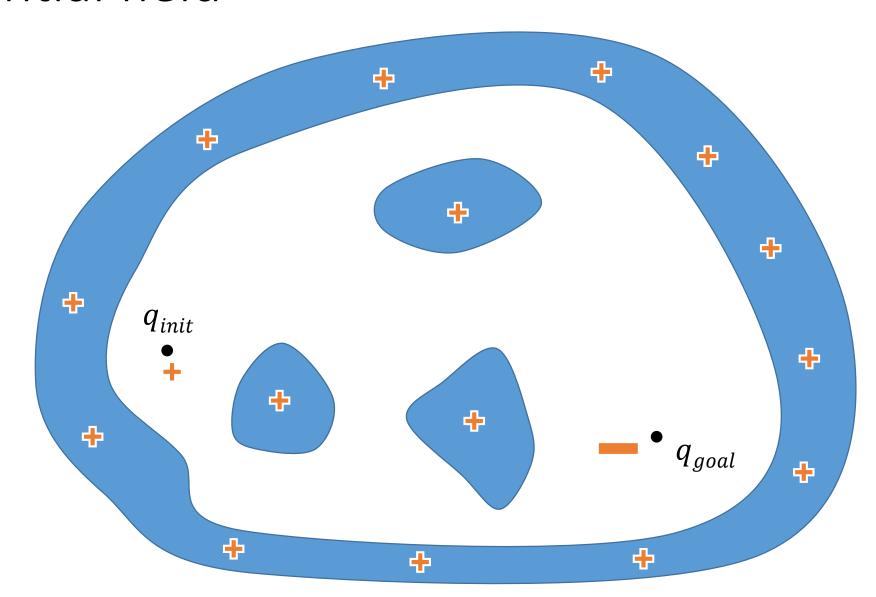
Bug algorithm

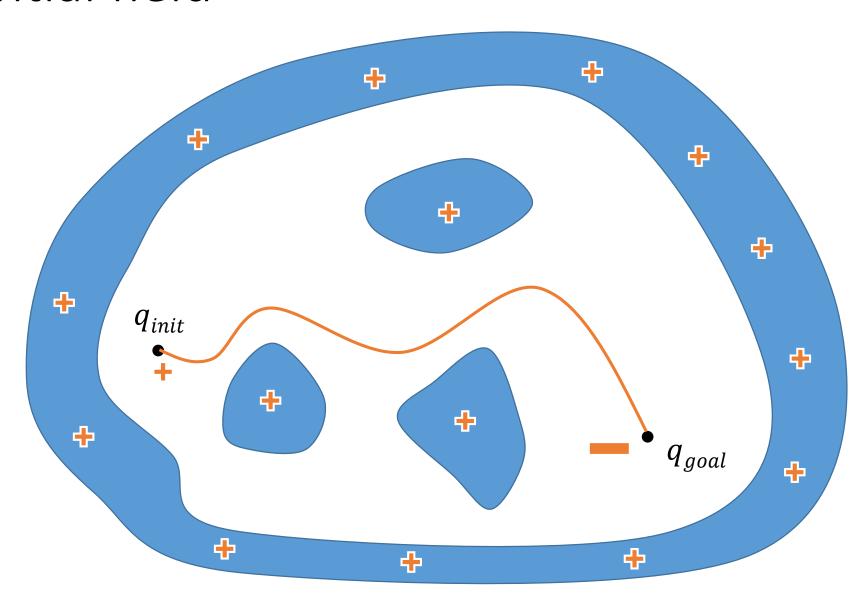


Bug algorithm

- Easy to find instances that "confuse the bug"
- We can add "memory" to the bug so that it circumvent all the obstacle before committing to leave it at best possible point
 - bug1 algorithm
- Add so-called m-line (straight line between initial and goal point through obstacles) as preferred direction to follow when leaving obstacle
 - bug2 algorithm
- "Cheating" → we allow ourselves to touch obstacles



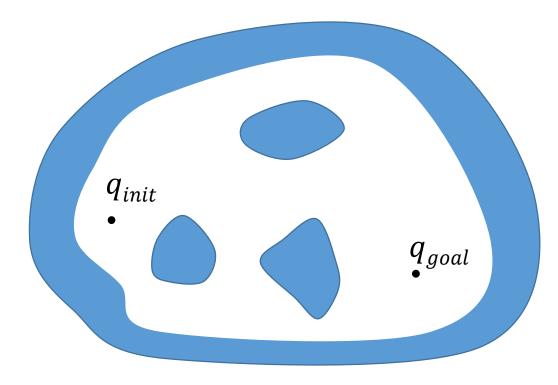




- Algorithm:
 - Charge particle and obstacles with given sign charge
 - Charge goal with opposite sign charge
 - Simulate the system and let it flow
- Problem: difficult to calibrate correctly the charges, the forces, etc, to avoid local minima in combined field (parameter tuning)
- Improvement : couple it with occasional local random walks when trapped in local minima

Google map meta algorithm

Can the Google maps meta-algorithm work here?

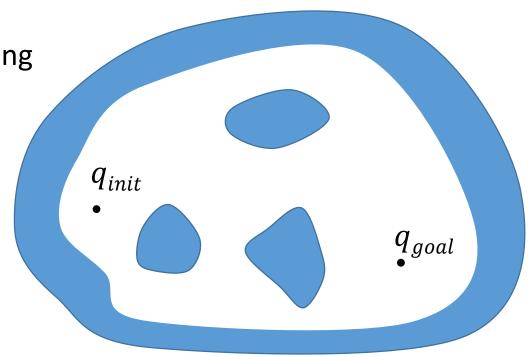


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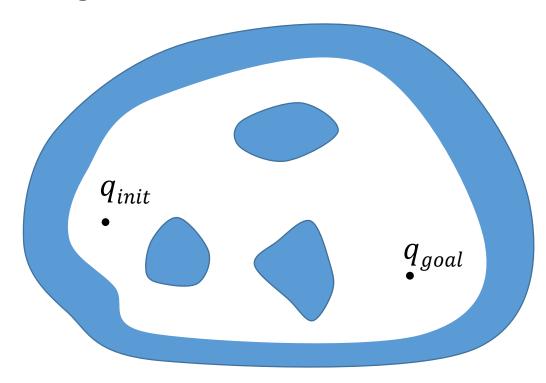
Yes if we can build a "roadmap"

• that is: a discrete structure (graph) encoding the connectedness of the free space

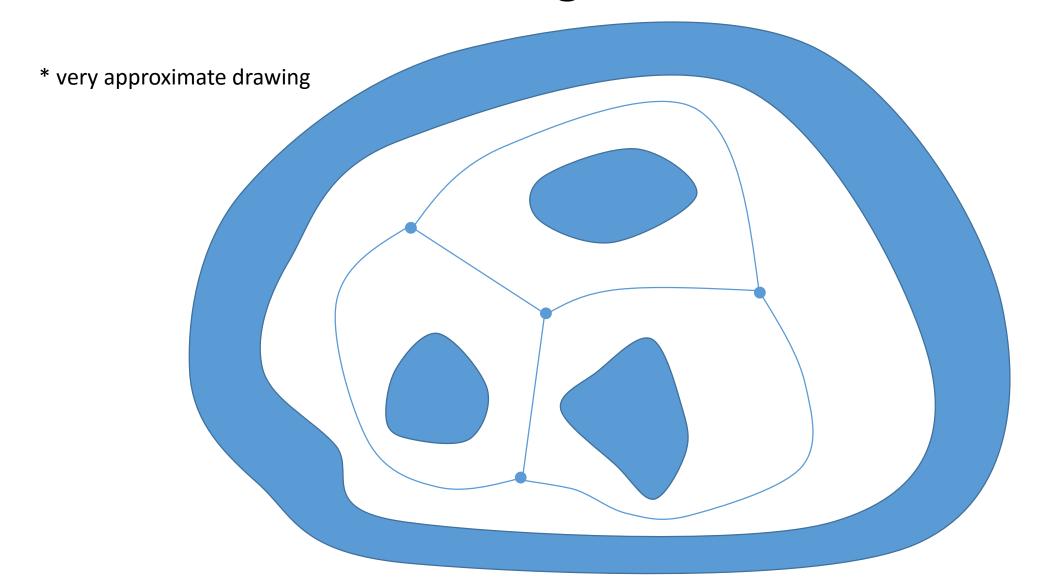


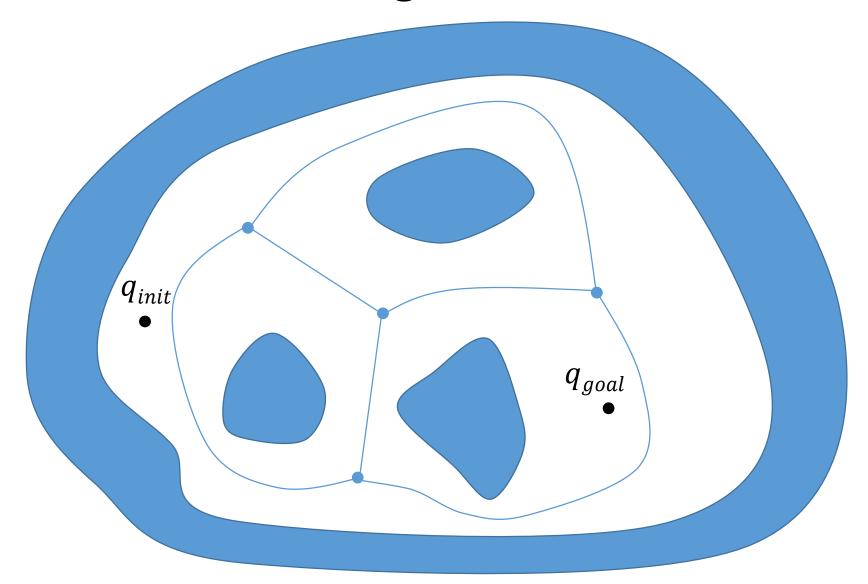
Google map meta algorithm

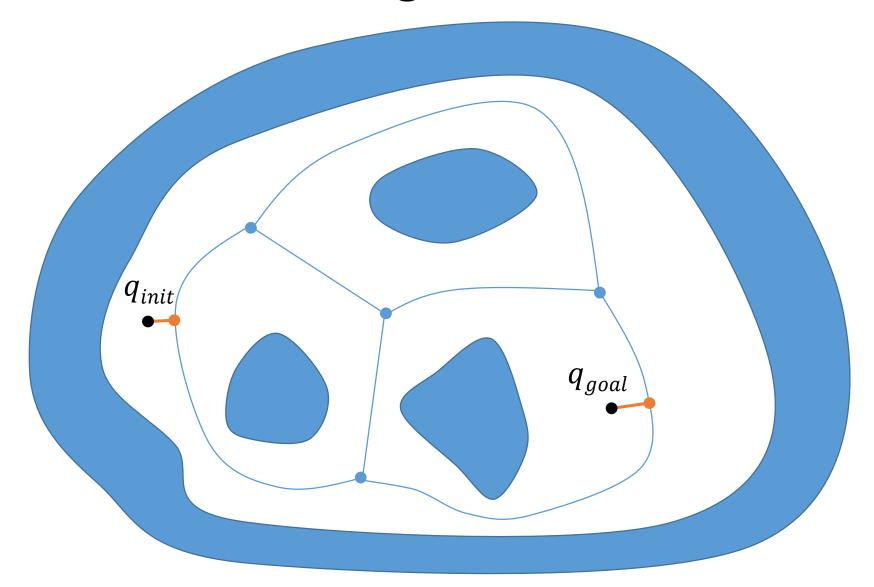
- Example algorithms for roadmap building:
 - Extended voronoi diagrams
 - Visibility roadmap
 - Cell decomposition
 - Exact cell decompositions
 - vertical cell decomposition
 - cylindrical cell decomposisition
 - Approximate cell decomposition
 - fixed resolution
 - adaptive resolution

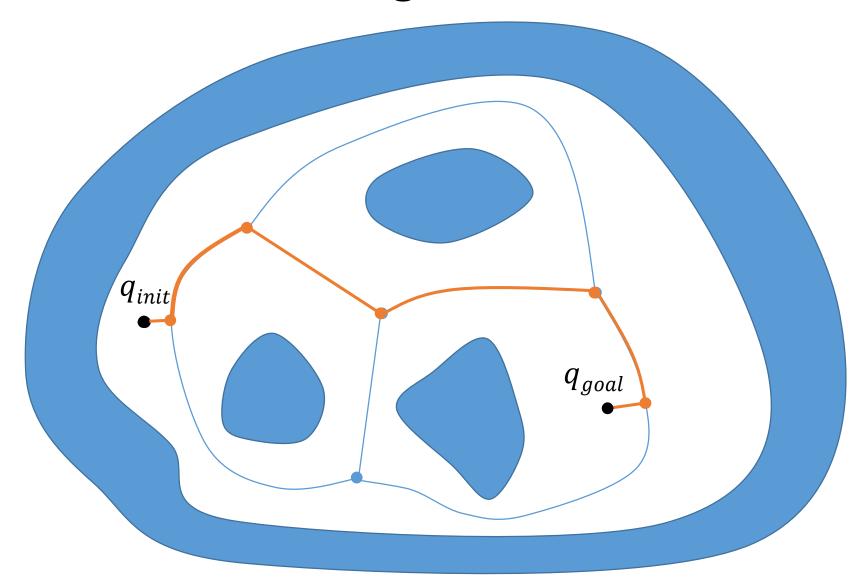




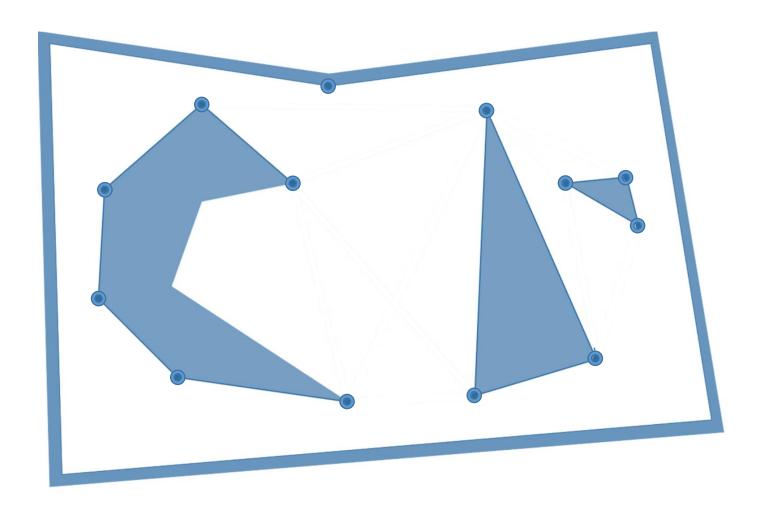






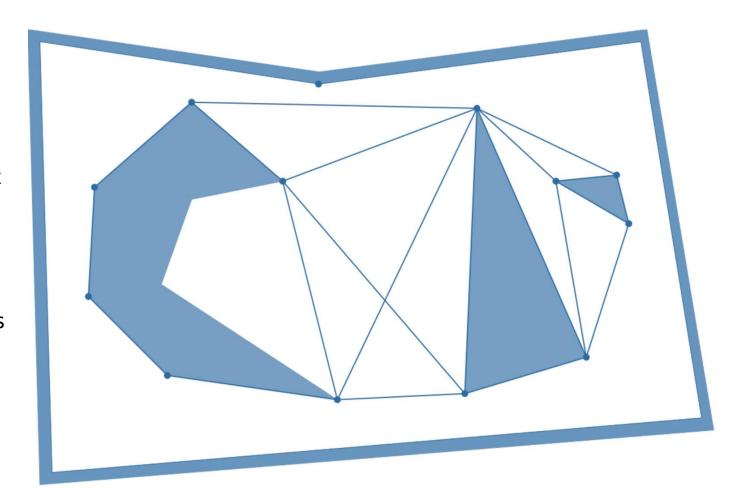


• Find reflex vertices (vertices where interior polygon angle are less than π

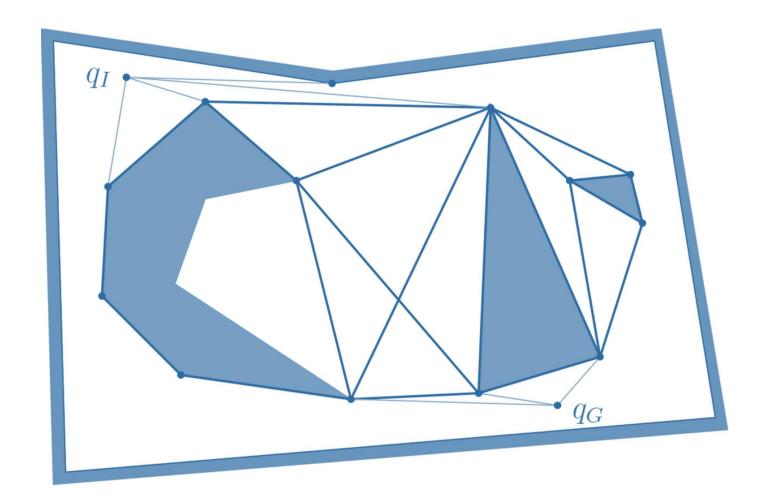


Connect:

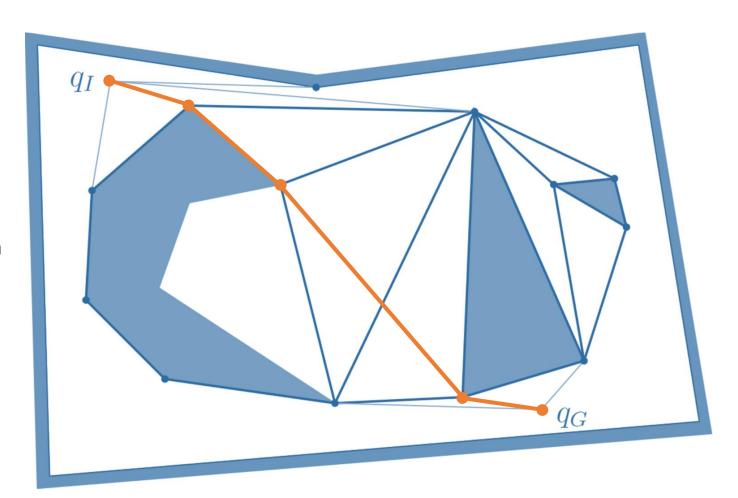
- consecutive reflex vertices on given polygon
- bitangeant edges
 (edges between
 two reflex vertices
 on different
 polygons such
 that both
 polygons are on
 the same side)



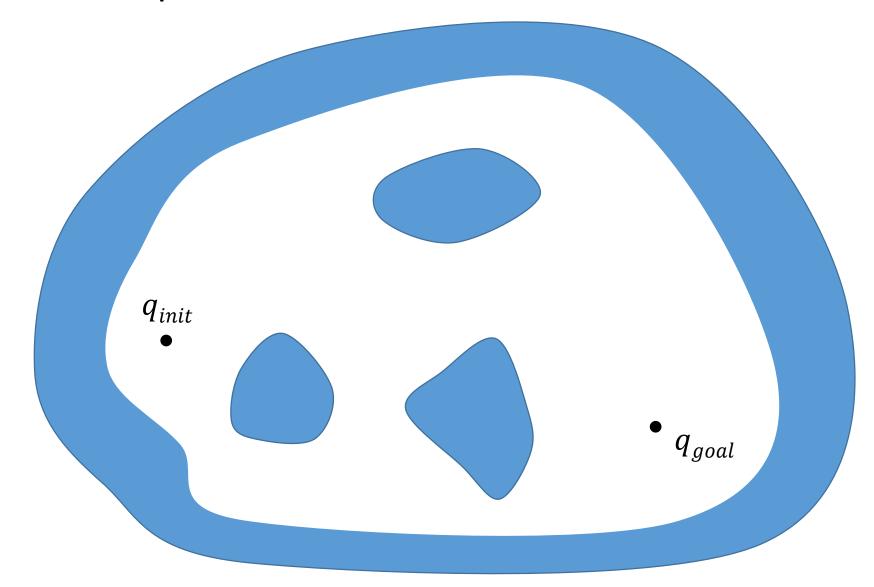
 Connect intial and goal points to all visible reflex vertices

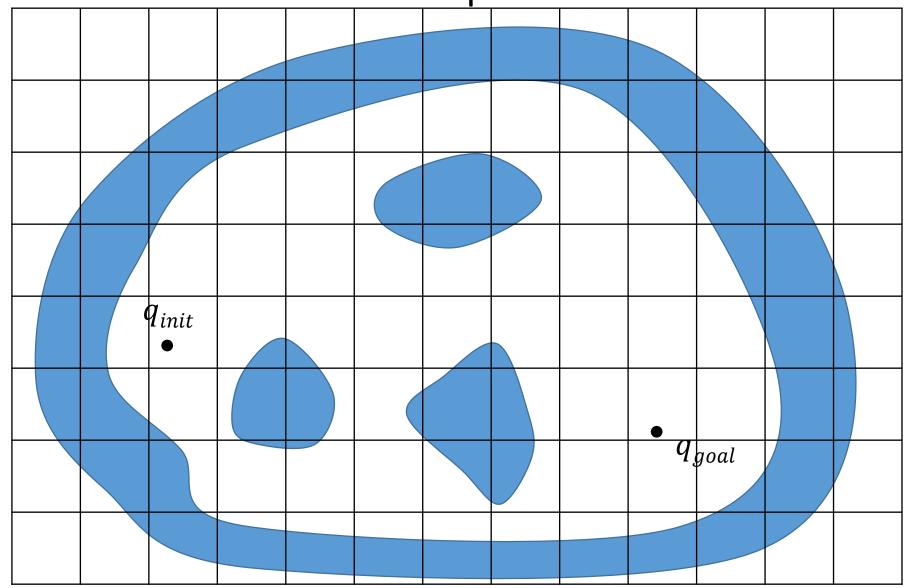


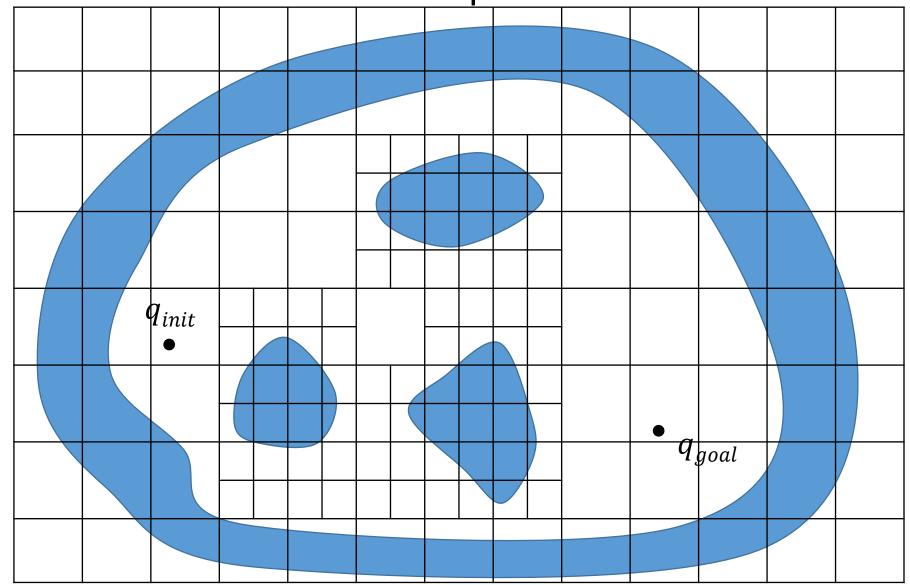
 run favorite graph search algorithm

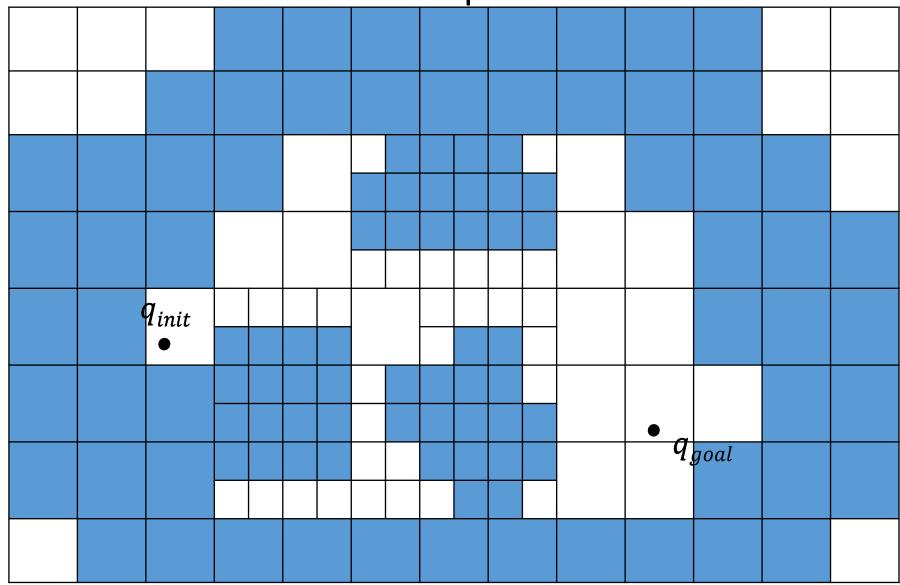


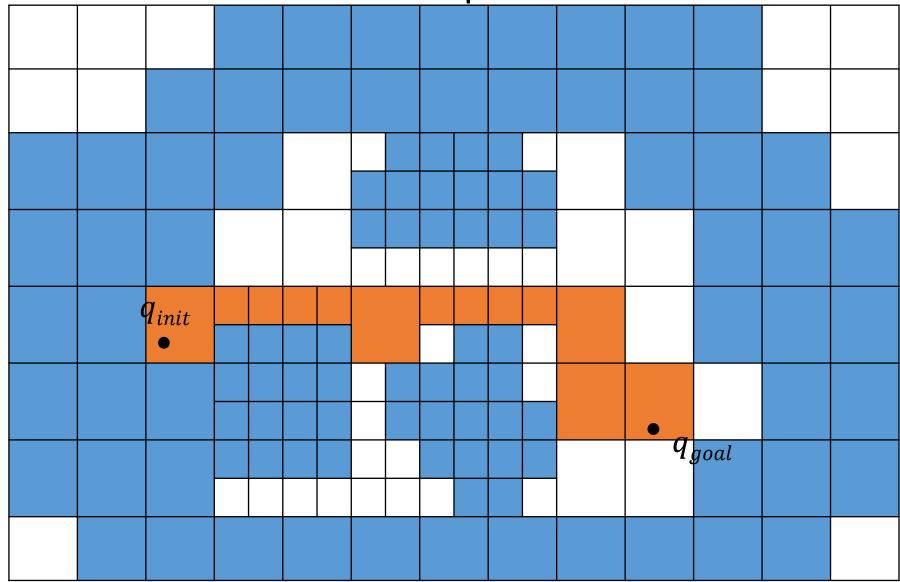
Cell decomposition

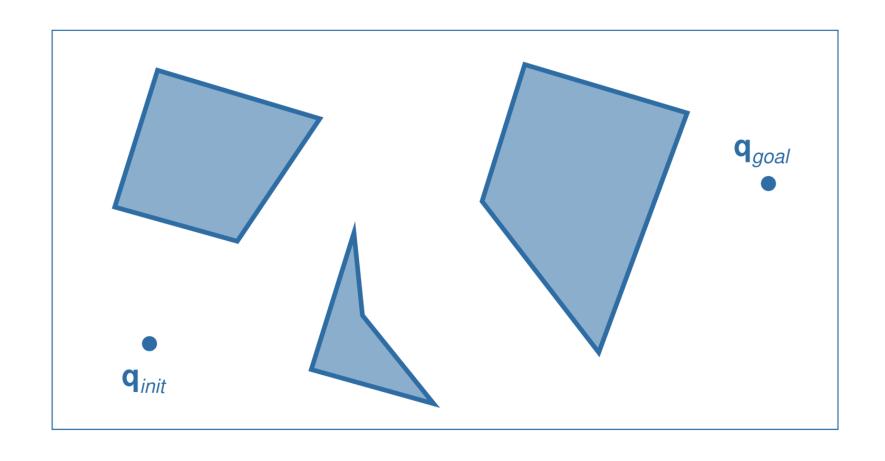


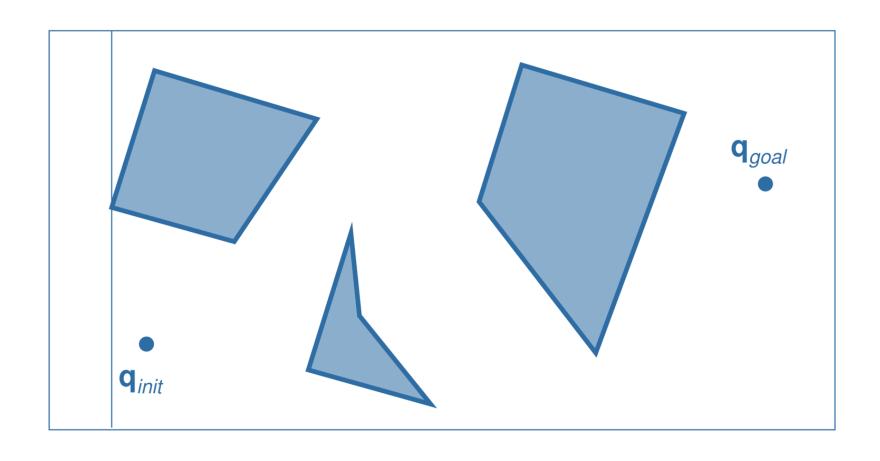


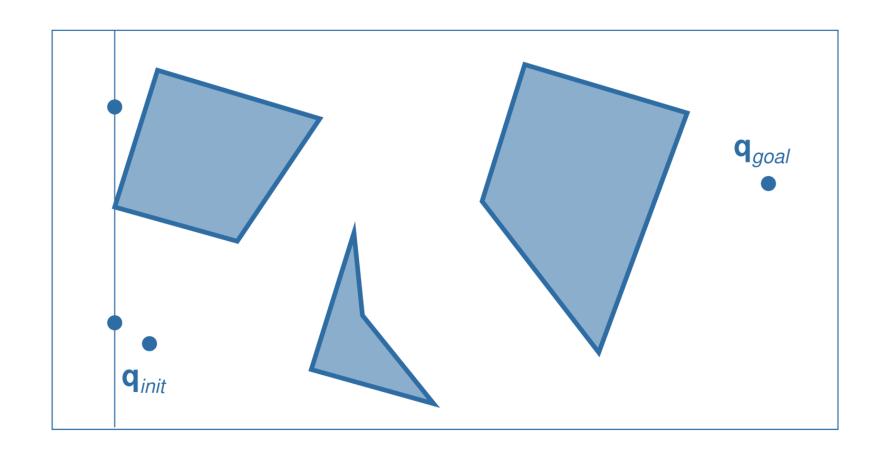


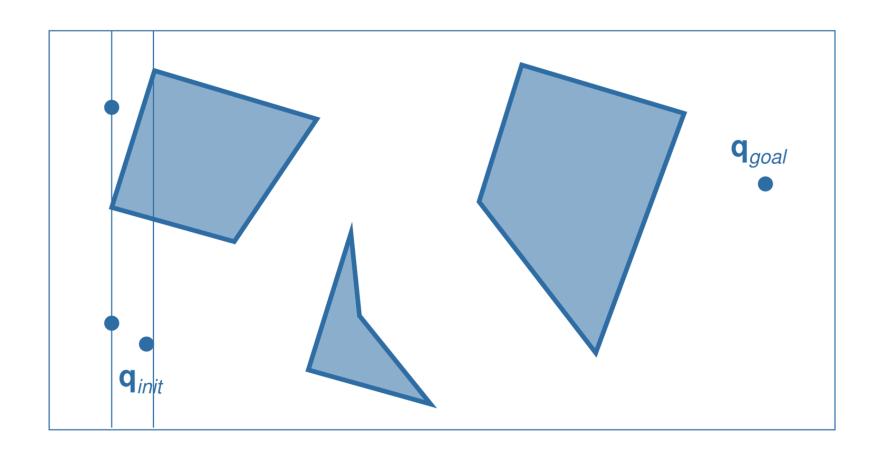


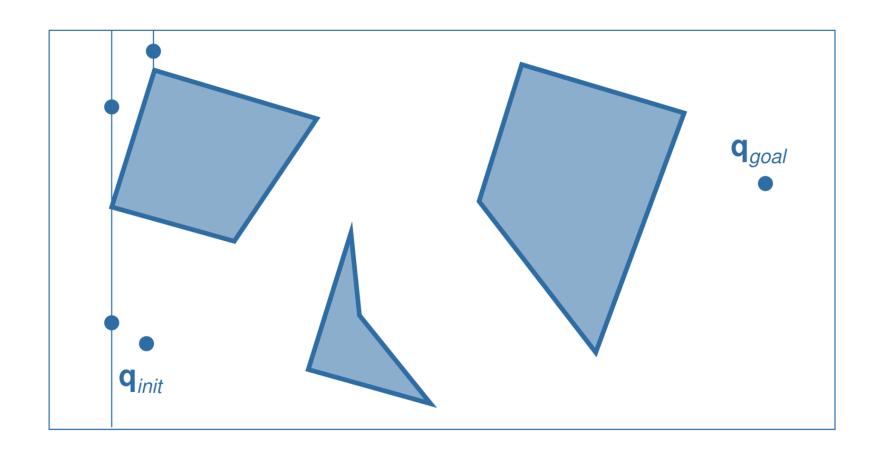


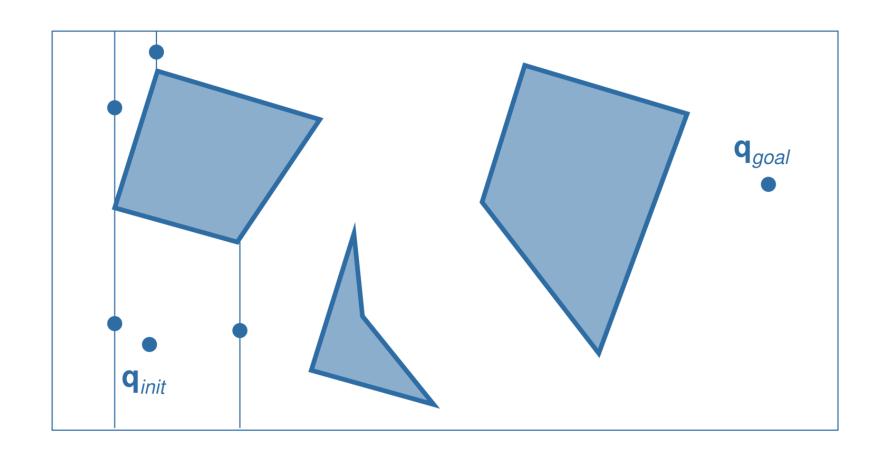


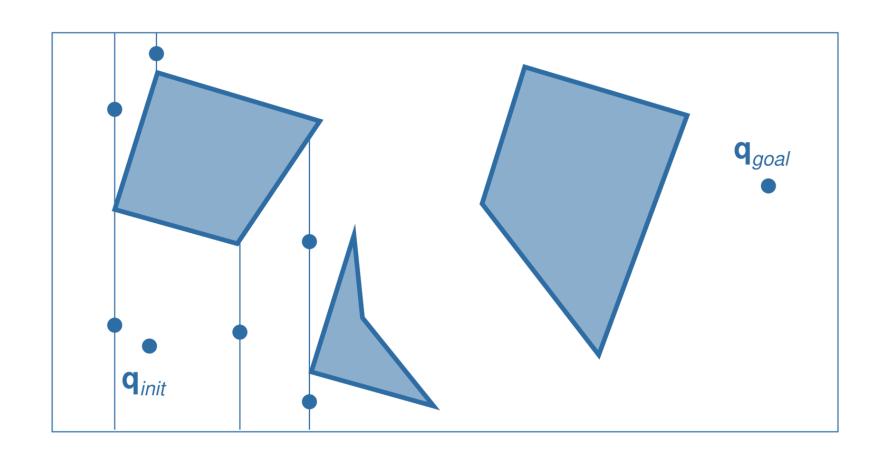


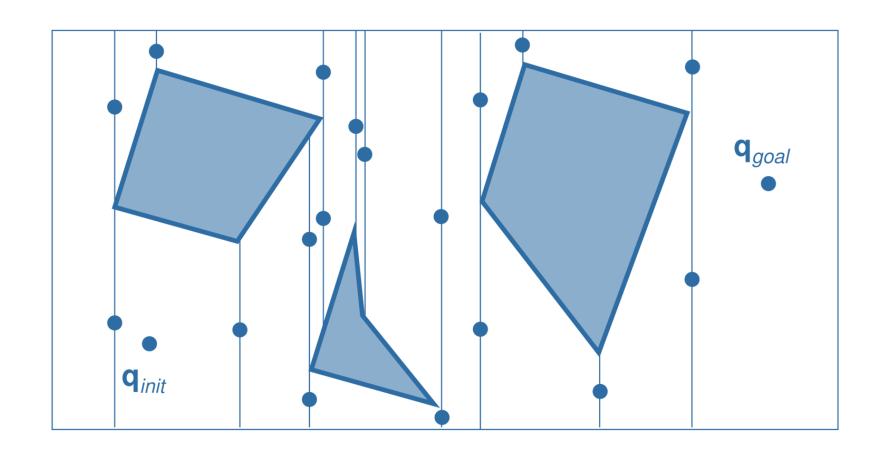


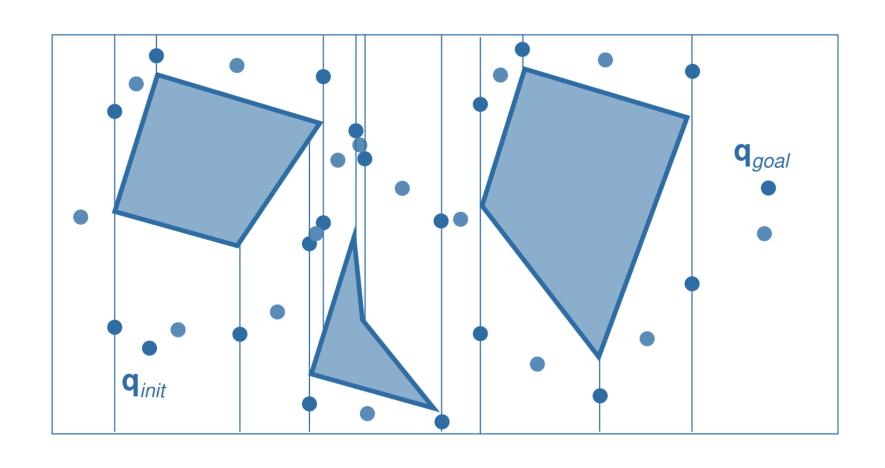


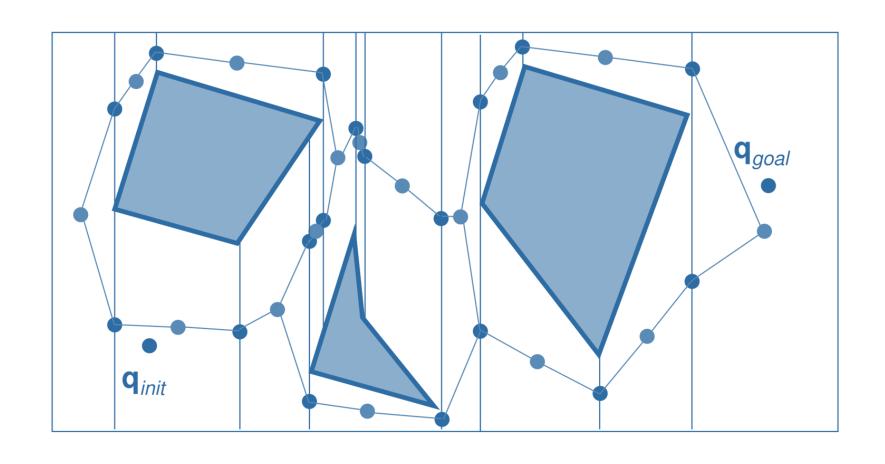


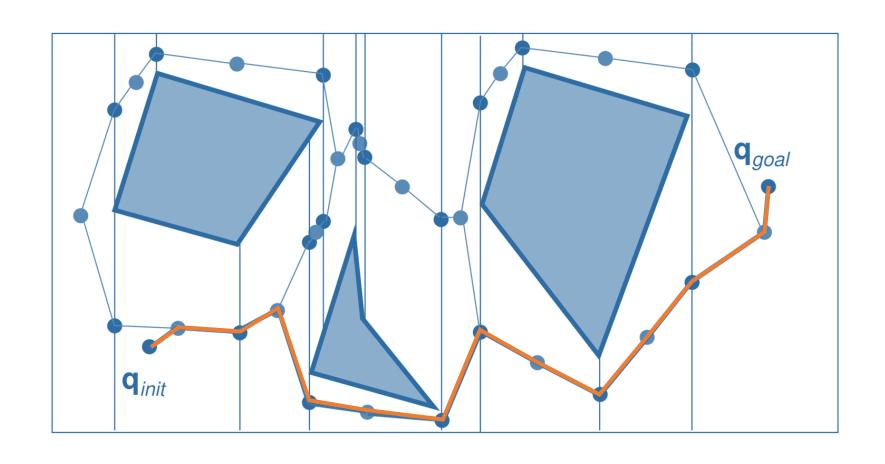




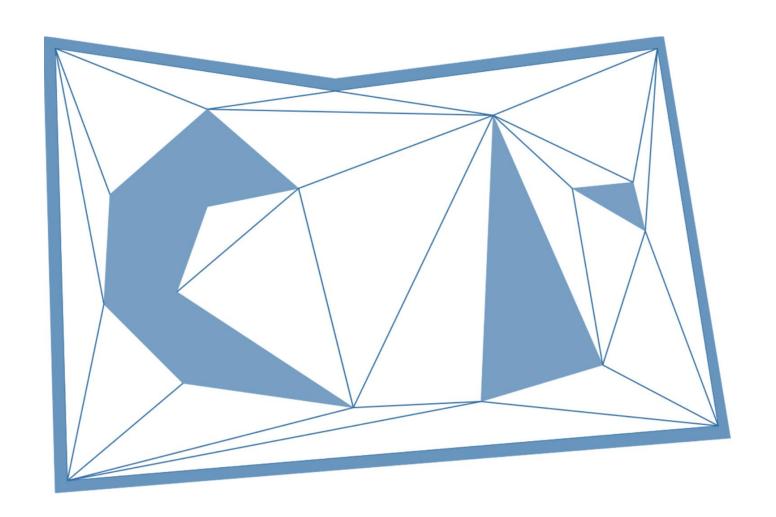




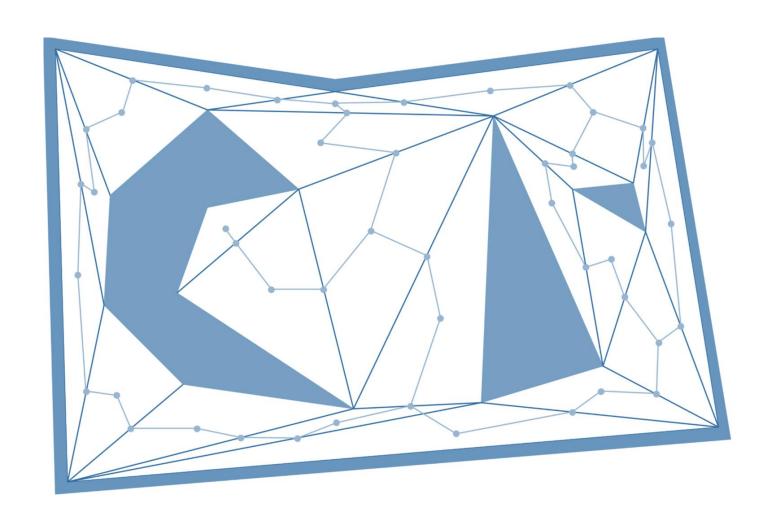




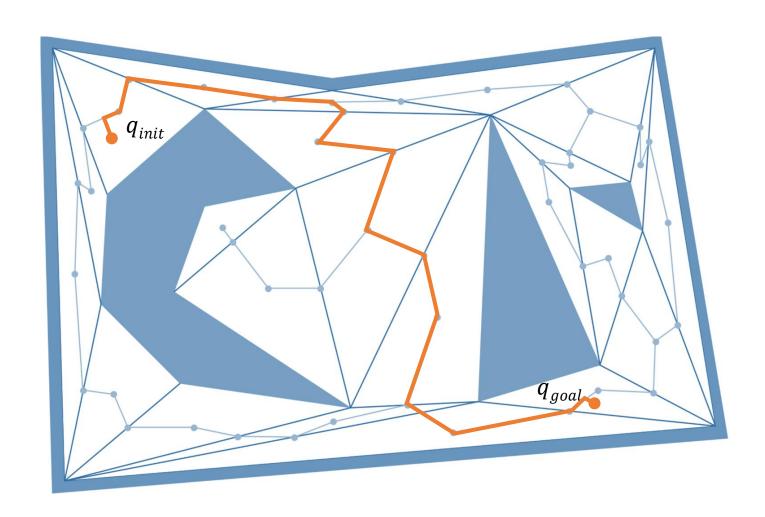
Triangulation



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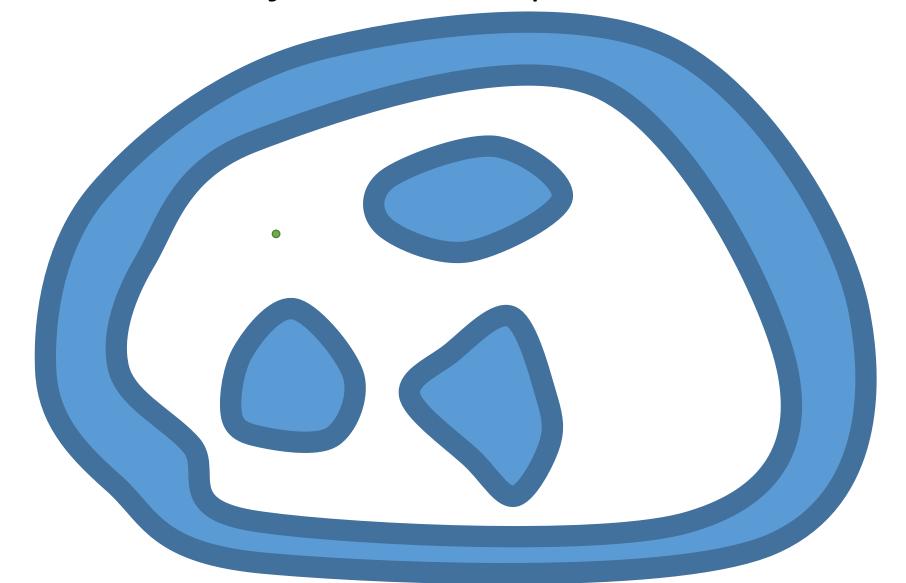


From path planning to motion planning

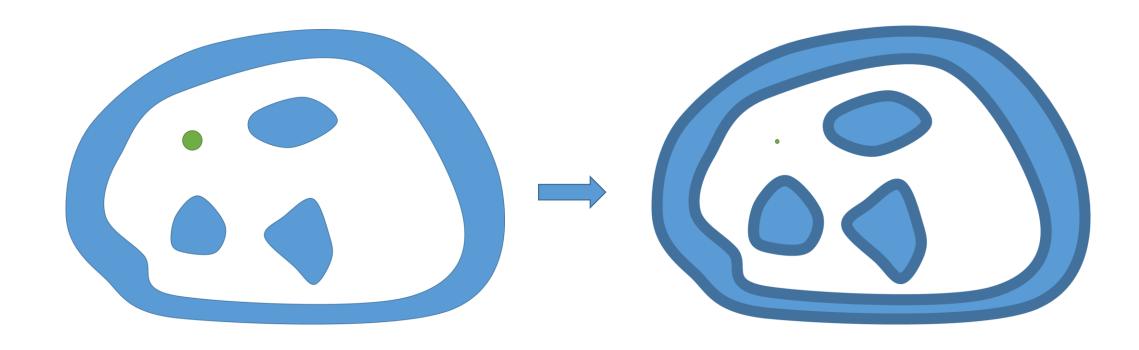
What if our subjet is not a point?

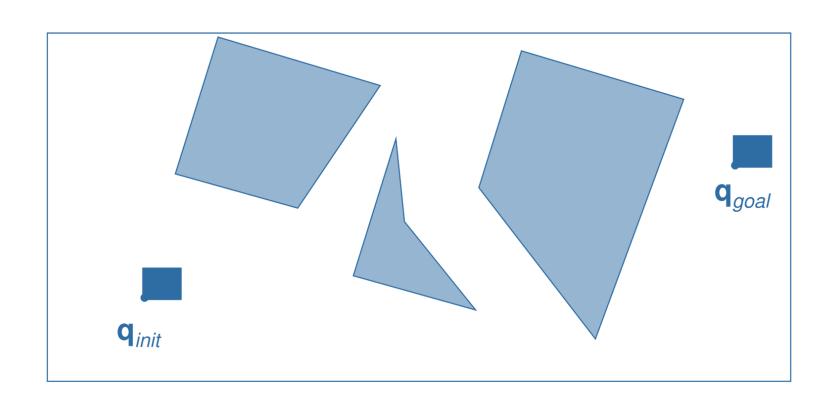


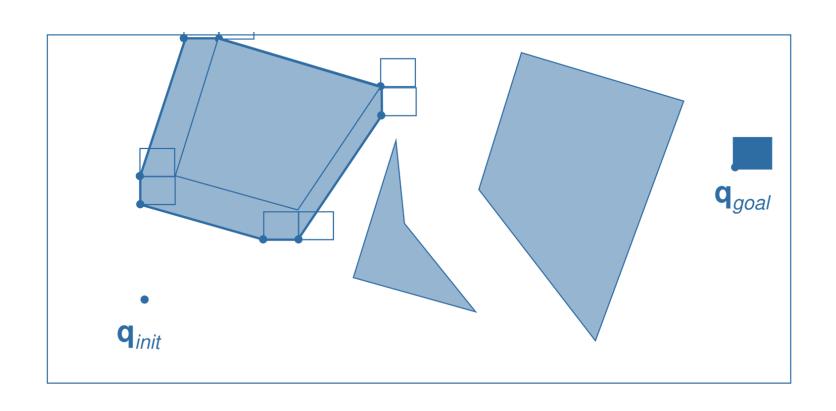
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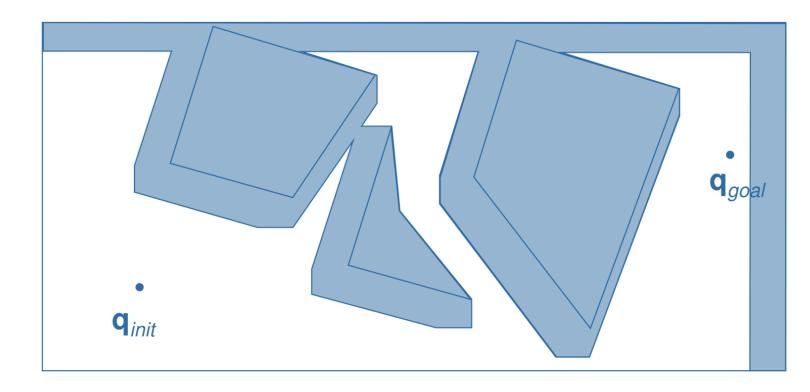
Towards motion planning



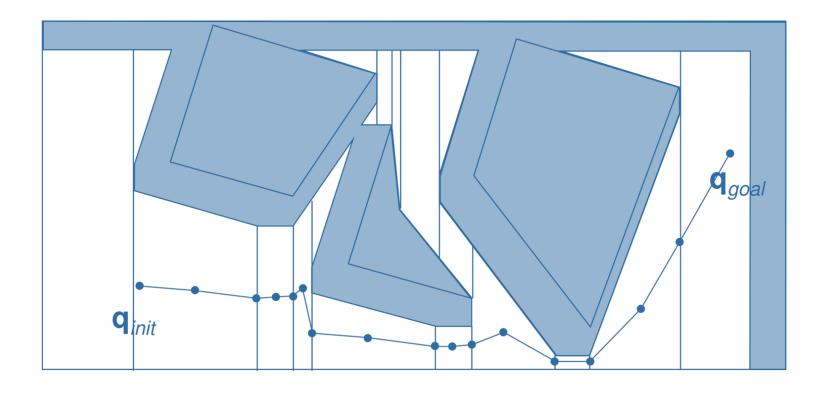




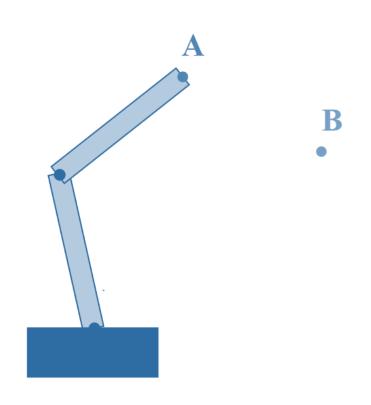
Replace subject with a point, and obstacles with Minkowski difference between obstacles and subject

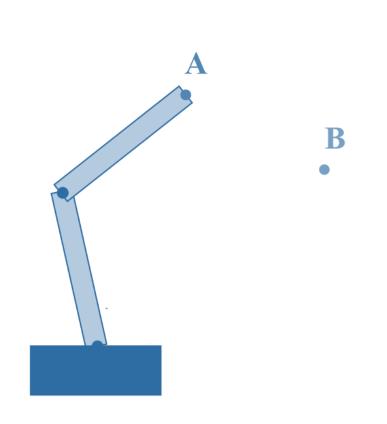


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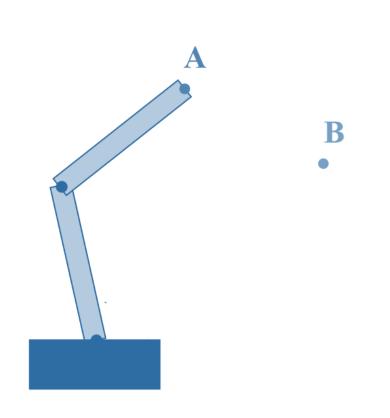
The motion planning problem as a path planning problem



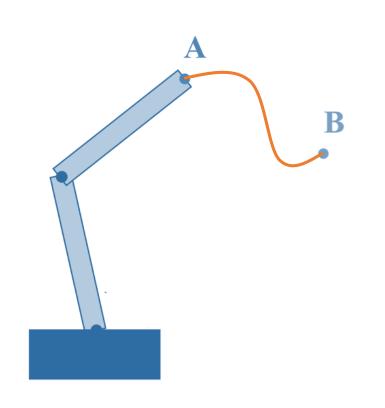


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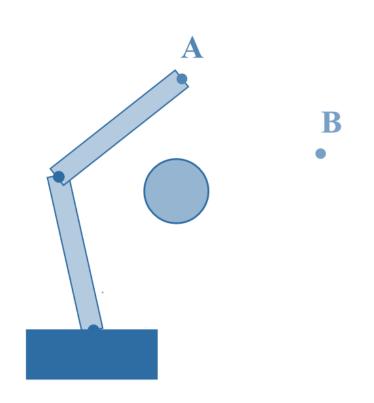
What is "go"?
what are "points" A and B?
"what" needs to go (subject of the verb)?



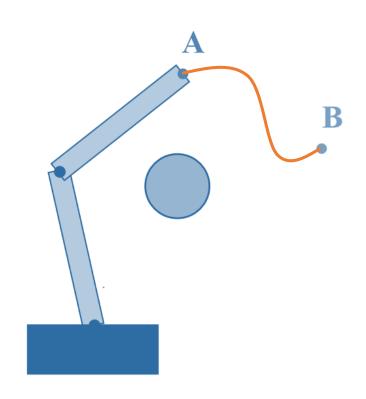
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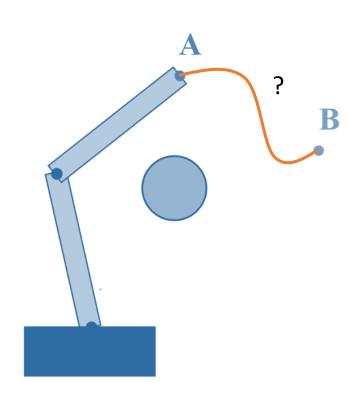
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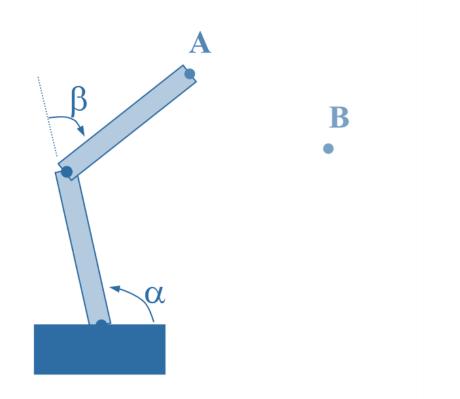
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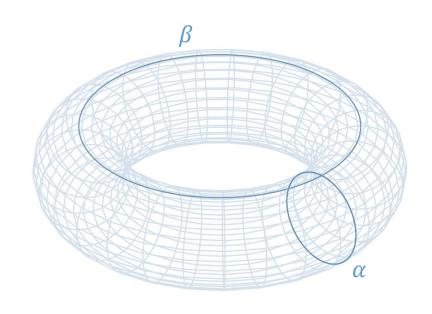


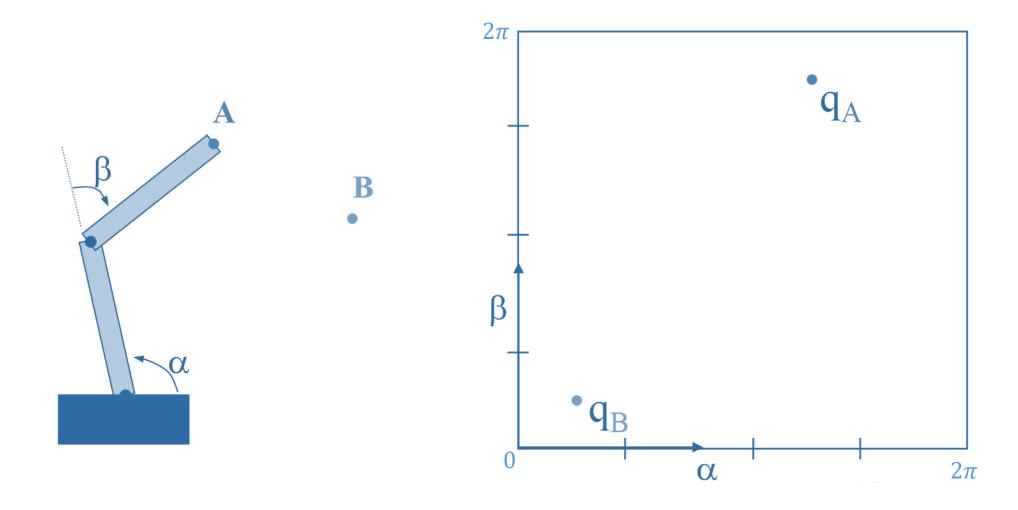
How to go from point A to point B?

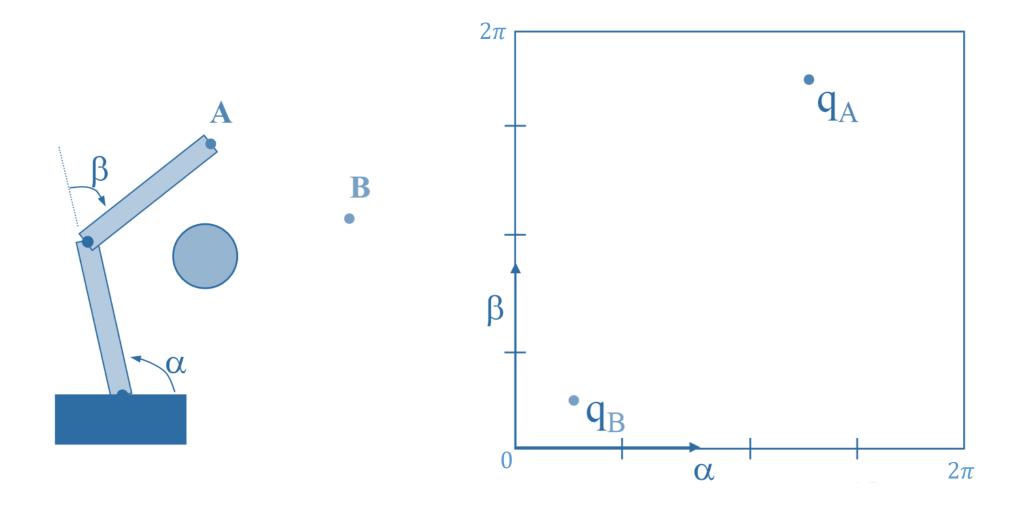
What is "go"? -> move the whole robot? what are "points" A and B? -> points of the 3D space? "what" needs to go (subject of the verb)? -> point on the robot?

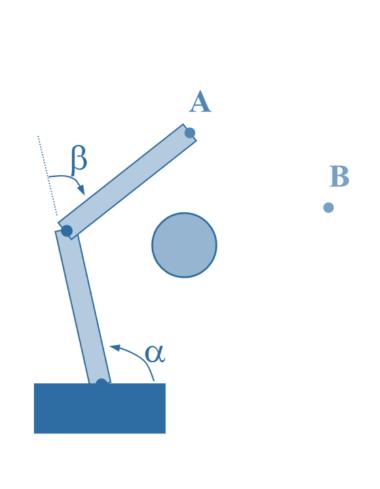
Definitely not a path planning problem from A to B

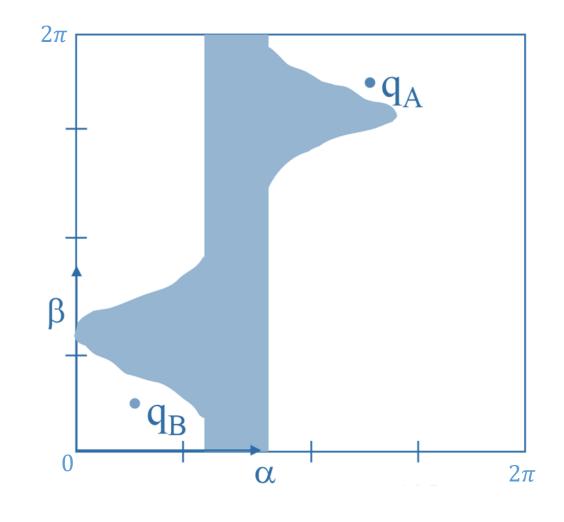


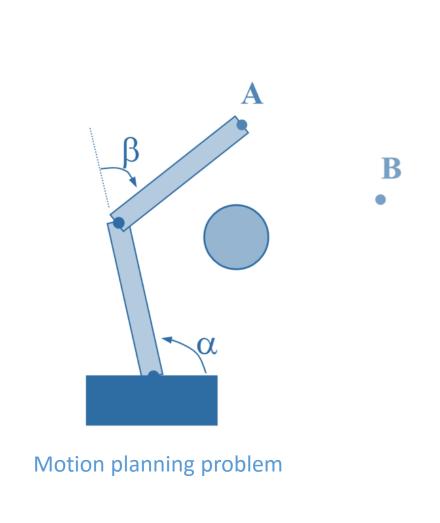


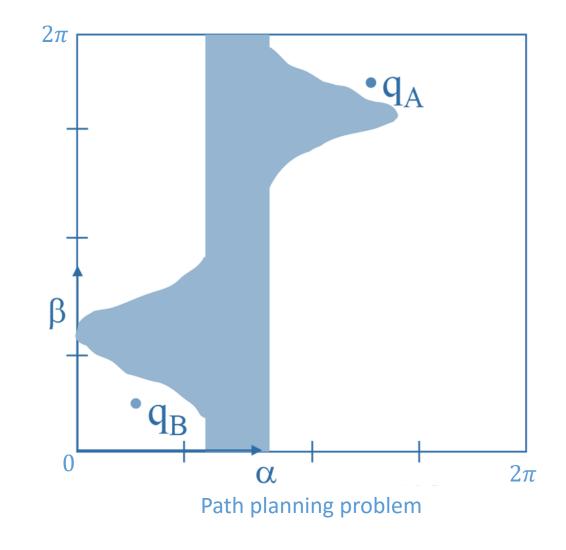


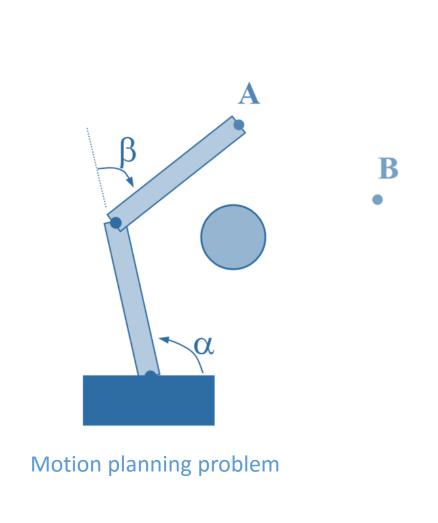


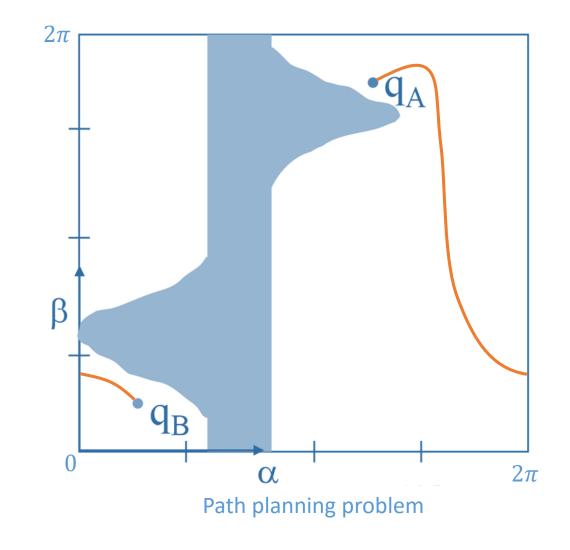












Configuration space ${\mathcal C}$

• point in \mathbb{R}^n :

• solid shape in 2D: $SE(2) = \mathbb{R}^2 \times SO(2) = \mathbb{R}^2 \times \mathbb{S}^1$

• revolute joint: \mathbb{S}^1 (circle)

• spherical joint: $SO(3) = \mathbb{RP}^3$ (real projective space) = unit quaternion hemisphere with antipodal identification

• solid shape in 3D: $SE(3) = \mathbb{R}^3 \times SO(3)$

• n-joint arm: $\mathbb{T}^n = \left(\mathbb{S}^1\right)^n$ (torus)

Formulation of the motion planning problem (aka the piano mover problem)

- A physical world $\mathcal{W}=\mathbb{R}^2$ or \mathbb{R}^3
- A robot $\mathcal{A} \subset \mathcal{W}$ as a collection of links with joint configuration $q \in \mathcal{C}$, where \mathcal{C} is a n-dimensional manifold
- a mapping $g: \mathcal{C} \to 2^{\mathcal{W}}$ (forward kinematics mapping) that puts the robot in a given configuration, for simplicity we denote g(q) as $\mathcal{A}(q)$
- A compact obstacle region $\mathcal{O} \subset \mathcal{W}$
- The motion planning problem for \mathcal{A} in \mathcal{W} amounts to a path planning problem in $C_{free} = C \setminus C_{obs}$ where $C_{obs} = \{q \mid \mathcal{A}(q) \cap \mathcal{O} \neq \emptyset\}$

Computational algebraic geometry solution to the problem

- Lemma: If we suppose that \mathcal{A} and \mathcal{O} are defined as semi-algebraic subsets of \mathcal{W} (ie defined using finite unions and intersections of regions delimited by polynomial equations with rational coefficients, including polygons/polyhedra, circles/spheres, ellipses/ellipsoids, etc), then it is possible to demonstrate that \mathcal{C}_{obs} and \mathcal{C}_{free} are also semi-algebraic subsets of \mathbb{R}^n for all types of robots with configuration spaces defined as finite Cartesian products of the previously listed manifolds.
- Example: polyhedral robots in polyhedral worlds

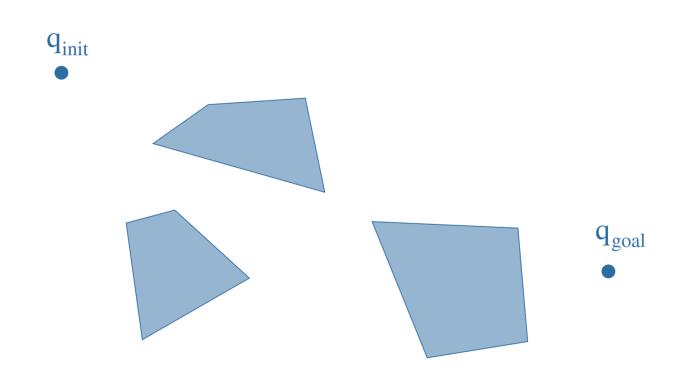
Computational algebraic geometry solution to the problem

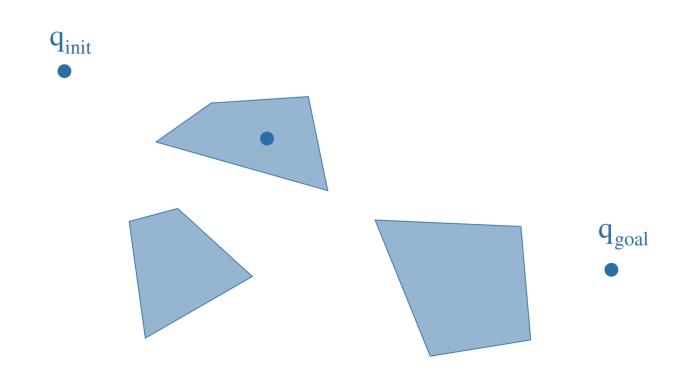
- Semi-algebraic regions are defined as Tarski sentences (logical predicates on polynomial expressions on manifold coordinates with quantifiers and free variables).
- The cylindrical algebraic decomposition (aka Collins decomposition) used for quantifier elimination in Tarski sentences (and for deciding satisfiability of Tarski sentences) yields in fact a cell decomposition of \mathcal{C}_{free} (similar to the vertical cell decomposition in the 2D polygonal case)
- Hence it solves the motion planning problem (Schwartz and Sharir, 1990)
- Complexity doubly exponential in the dimension n

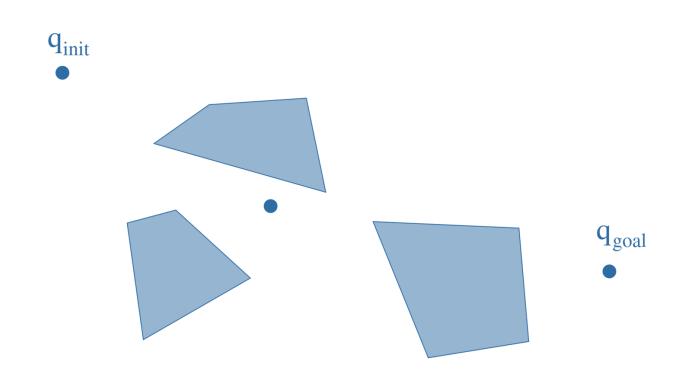
So, are path planning algorithms applicable to the motion planning problem?

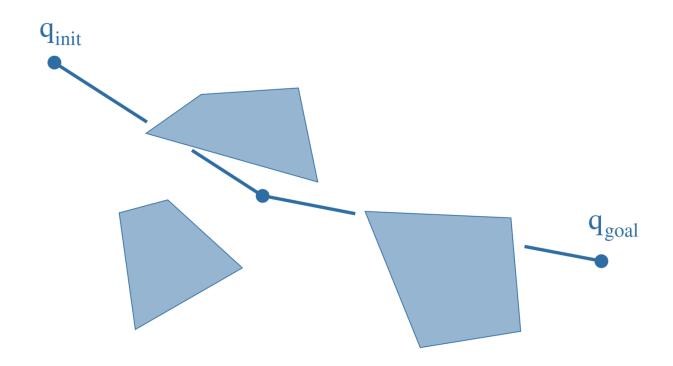
- Problem 1: many of the presented path planning algorithms make assumptions on the nature of the obstacle region (e.g. polygons). Eventhough we can make such assumptions on \mathcal{O} , it is difficult to say anything about the shape of \mathcal{C}_{obs}
- Problem 2: many of the presented path planning algorithms require explicit computation of the obstacle region. Again, it is difficult to compute explicitly \mathcal{C}_{obs}
- Problem 3: supposing 1 and 2 are solved, many of the presented path planning algorithms don't scale well beyond 2 or 3 dimensions (typical robot arm has 6 dof)

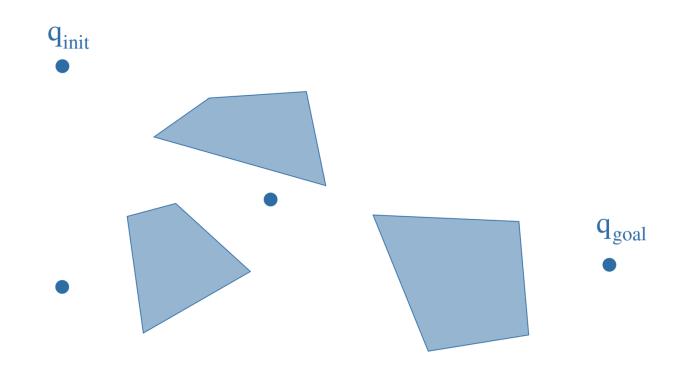
Sampling-based approaches

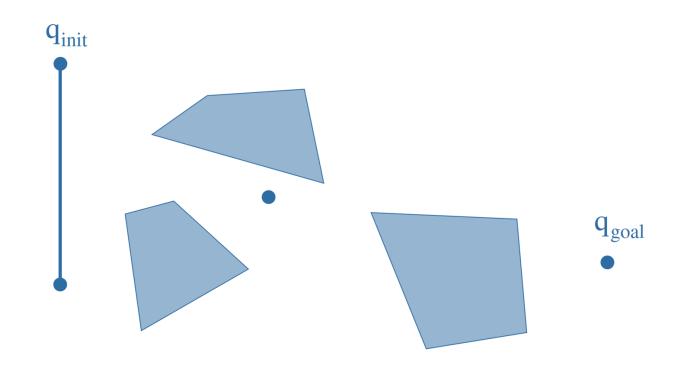


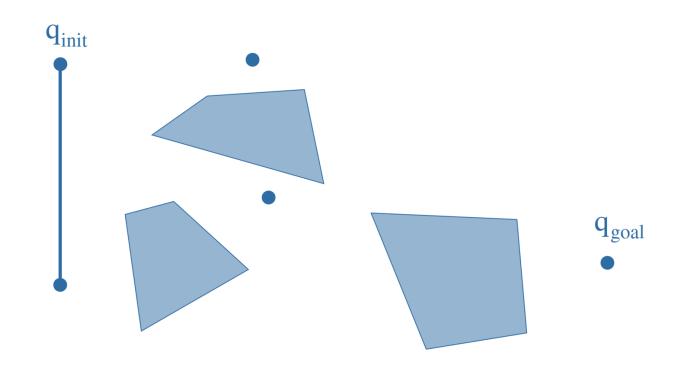


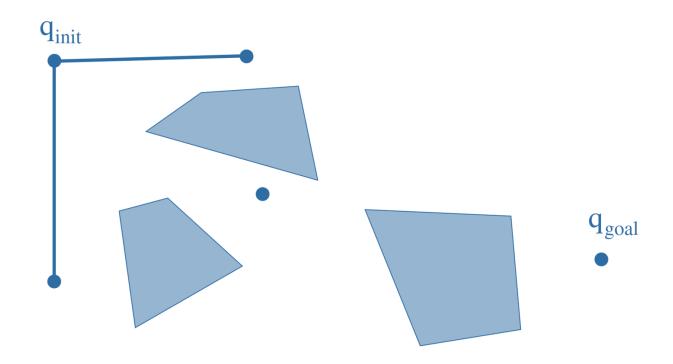


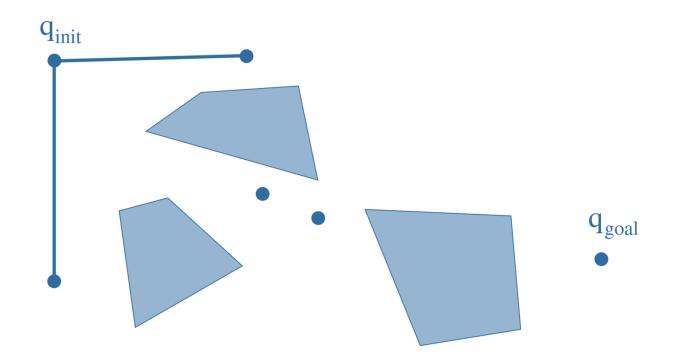


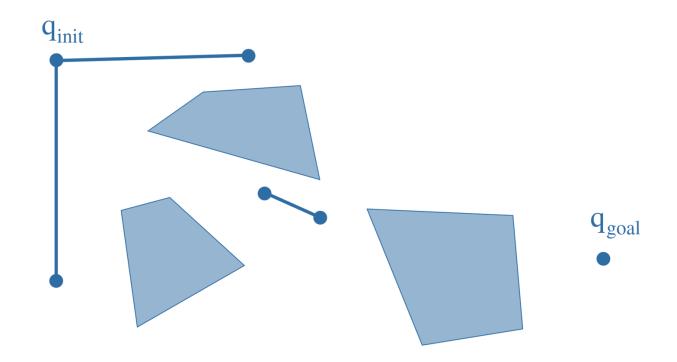


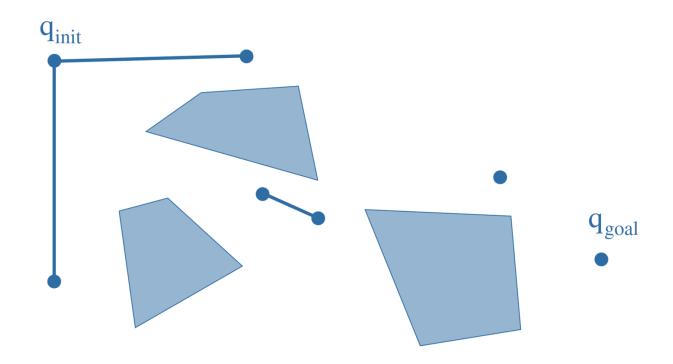


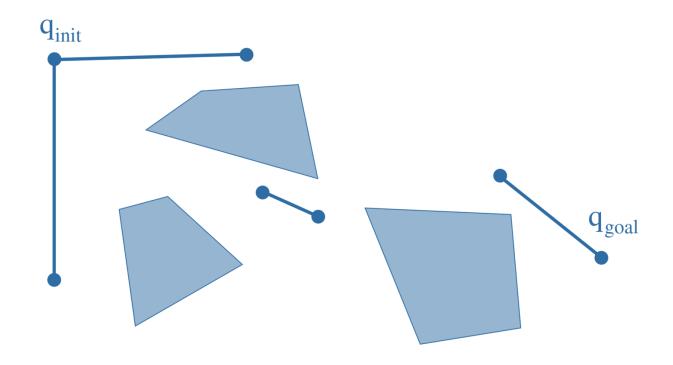


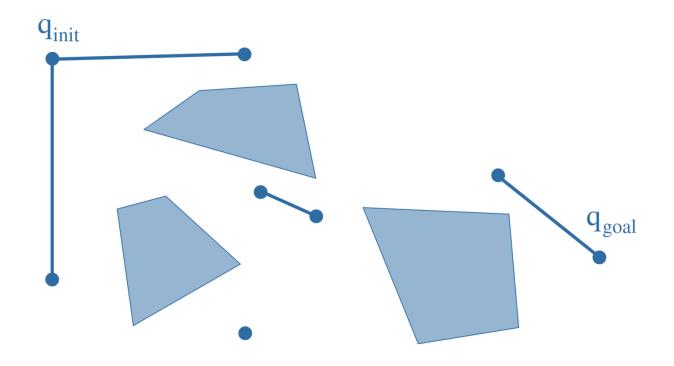


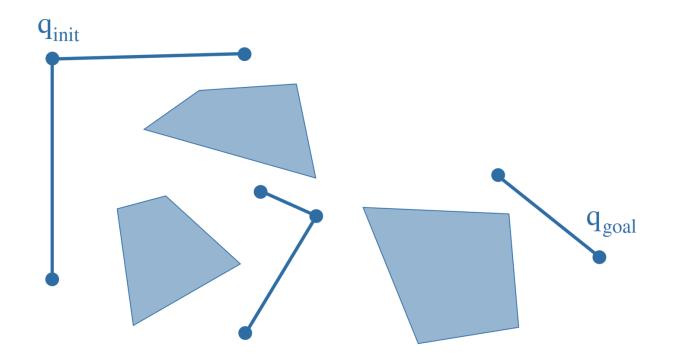


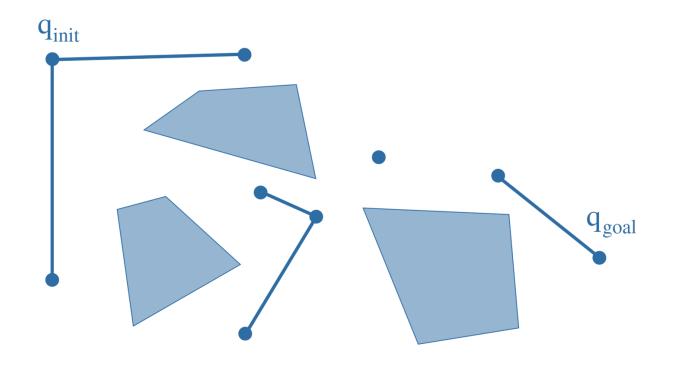


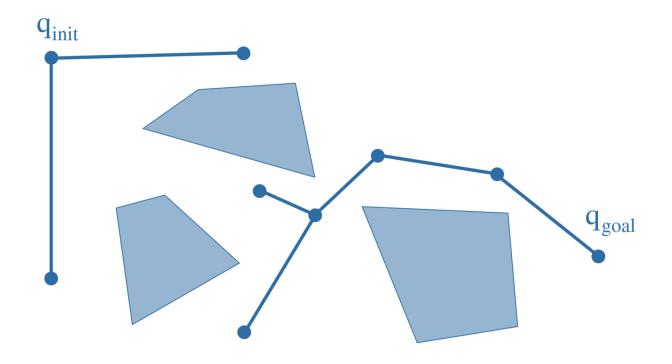




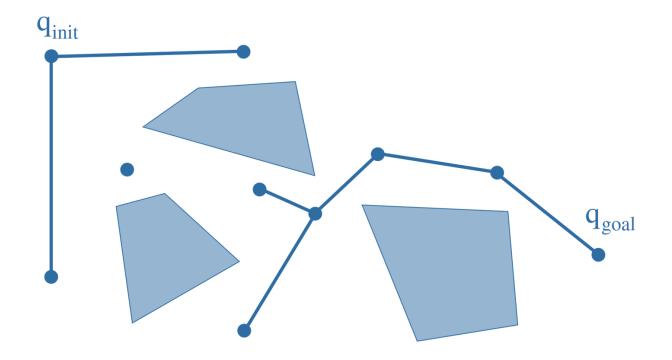




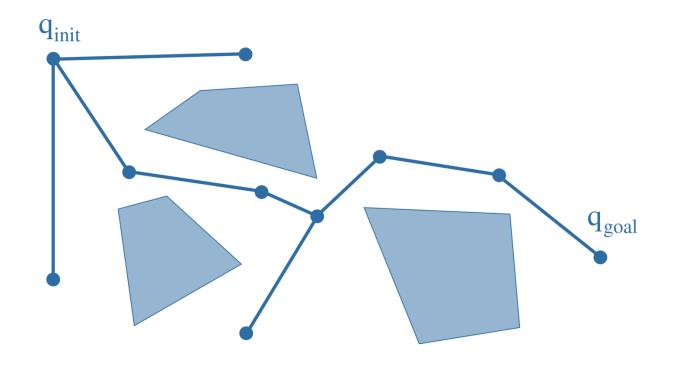




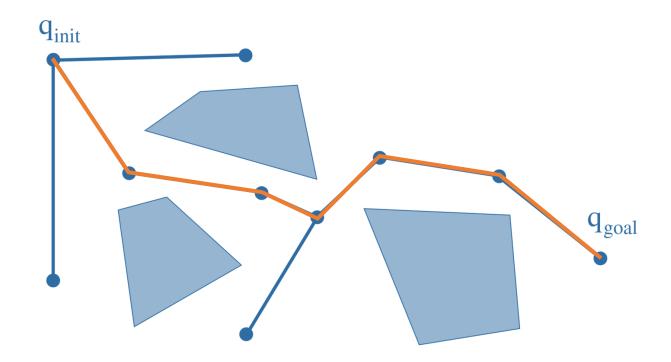
Probabilistic roadmap (PRM)

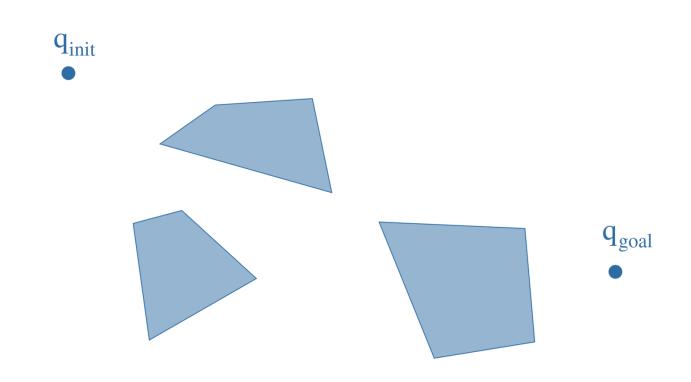


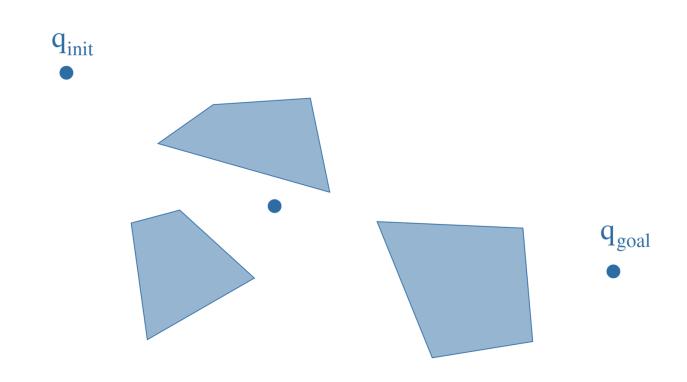
Probabilistic roadmap (PRM)

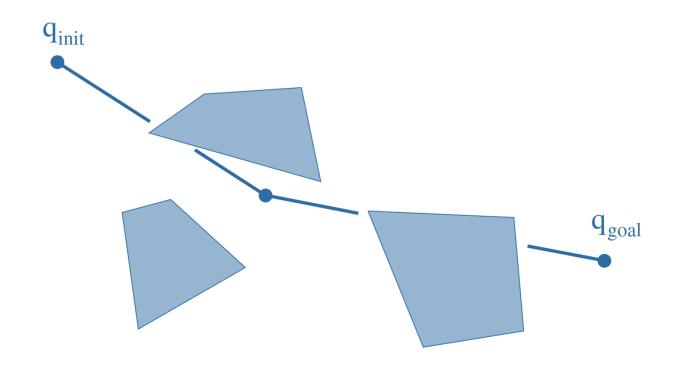


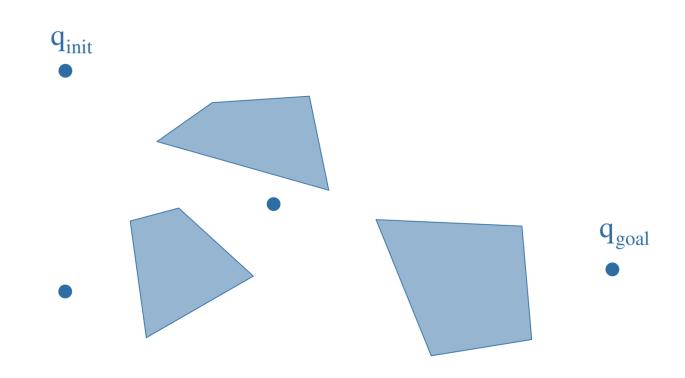
Probabilistic roadmap (PRM)

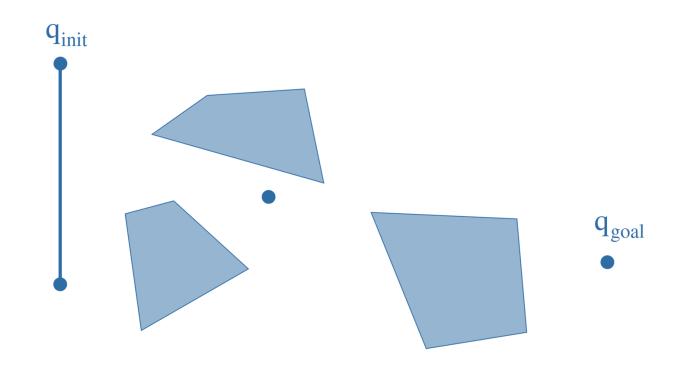


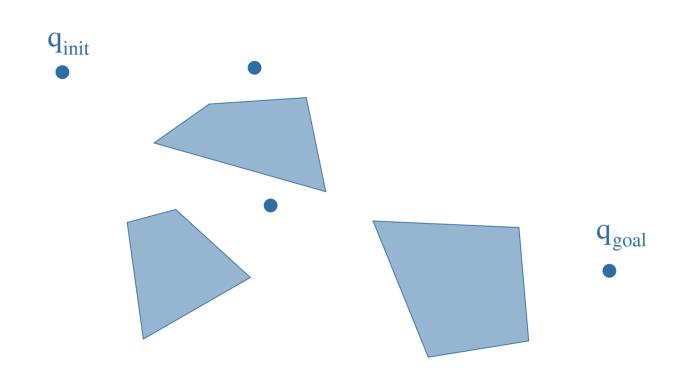


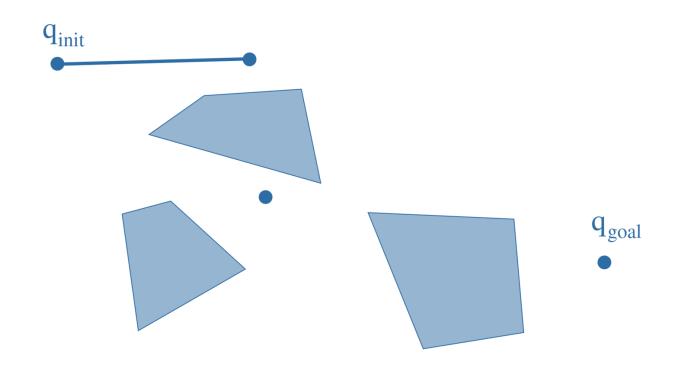


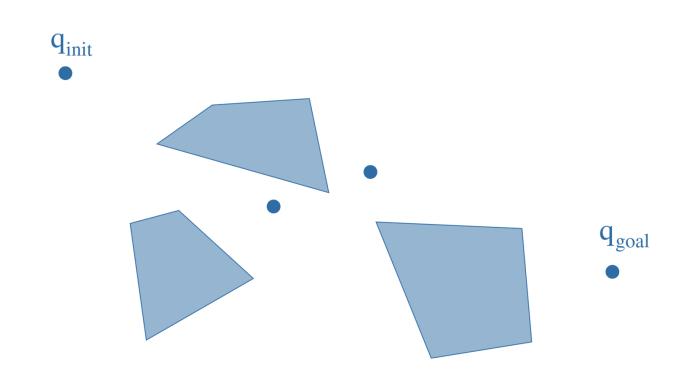


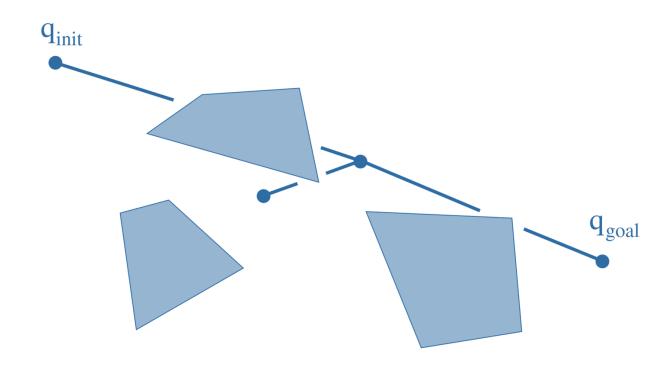


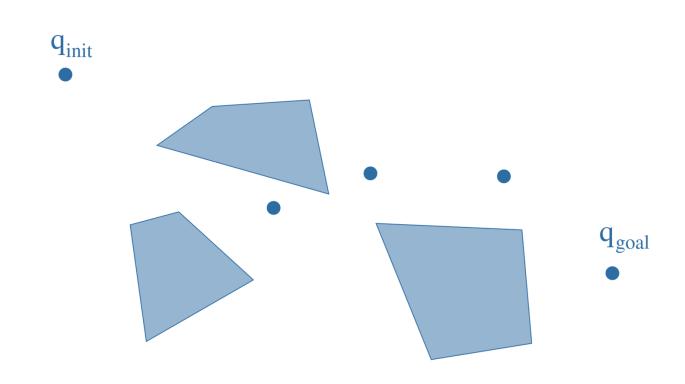


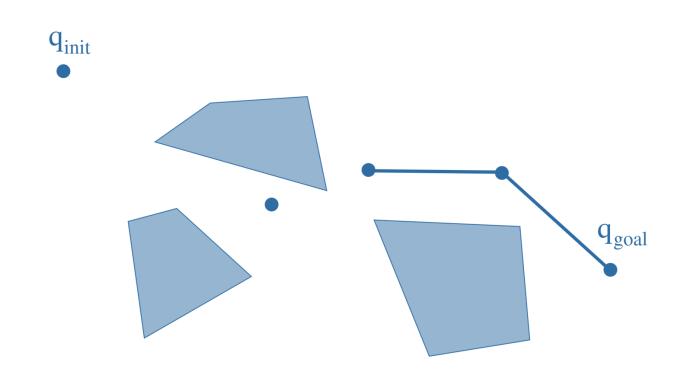


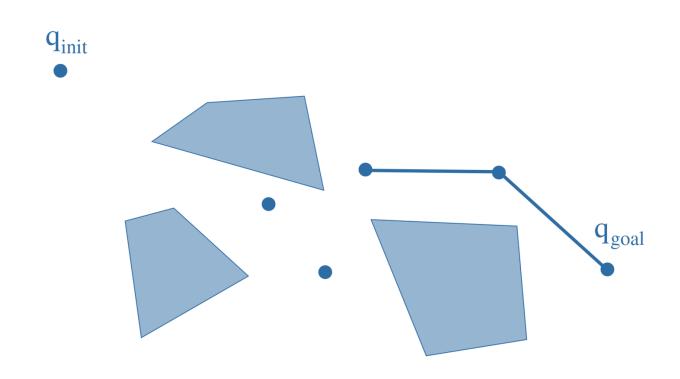


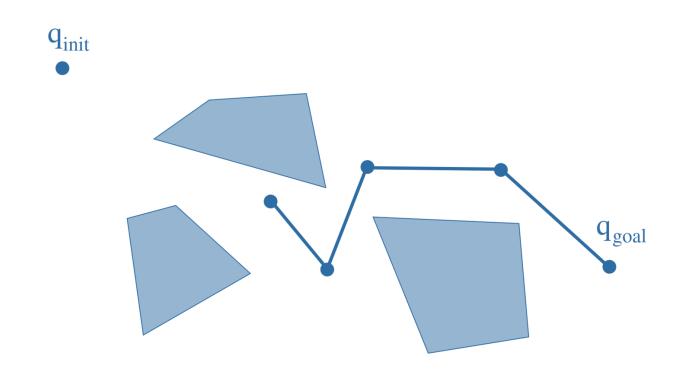


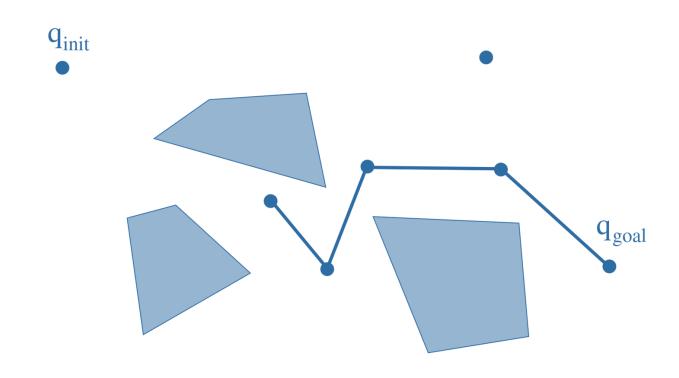


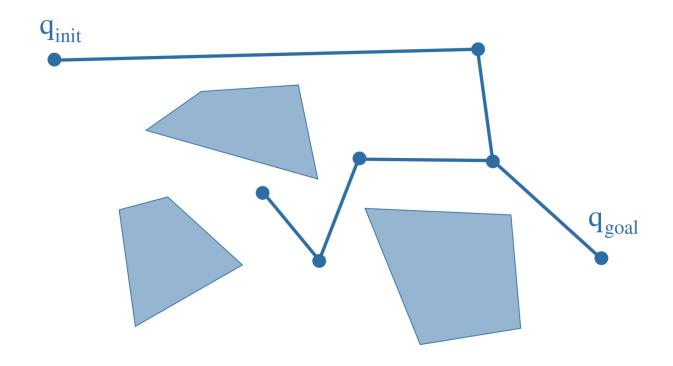


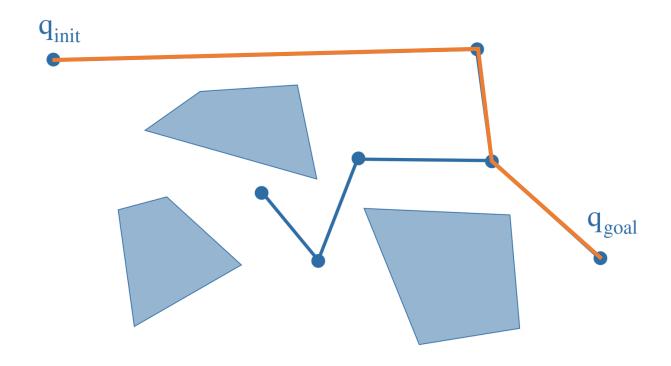


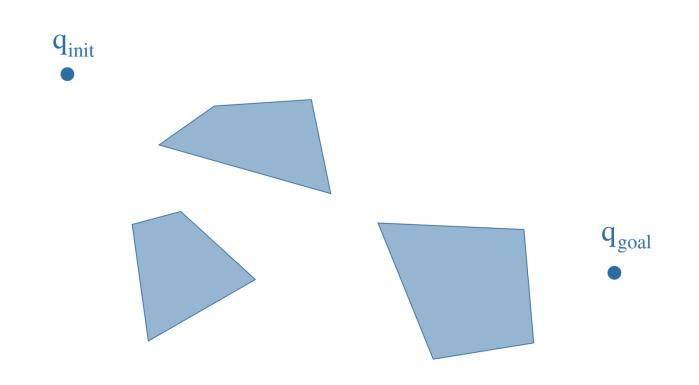


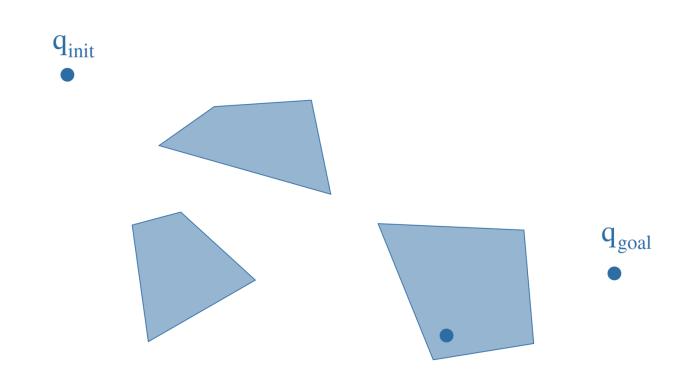


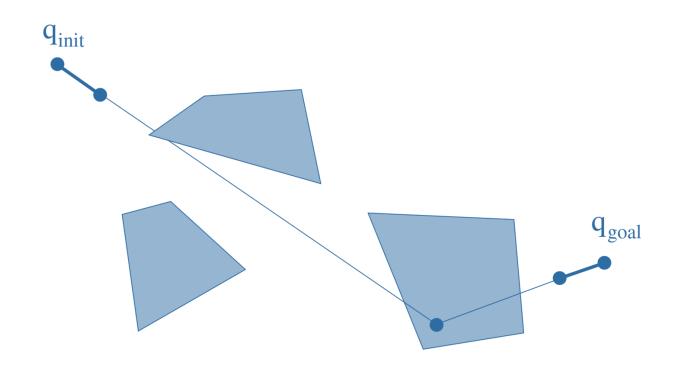


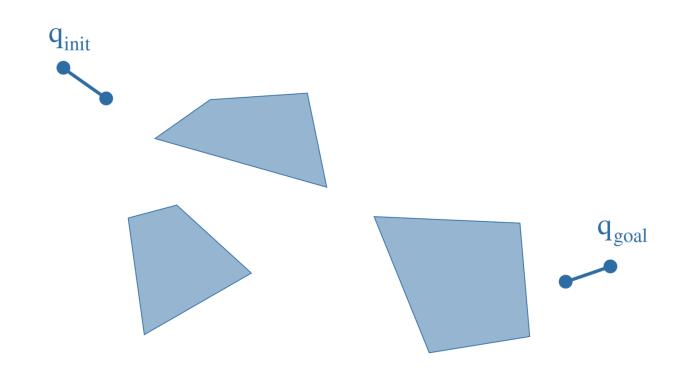


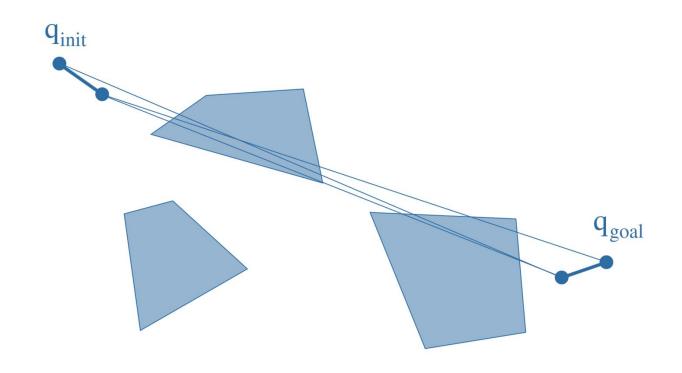


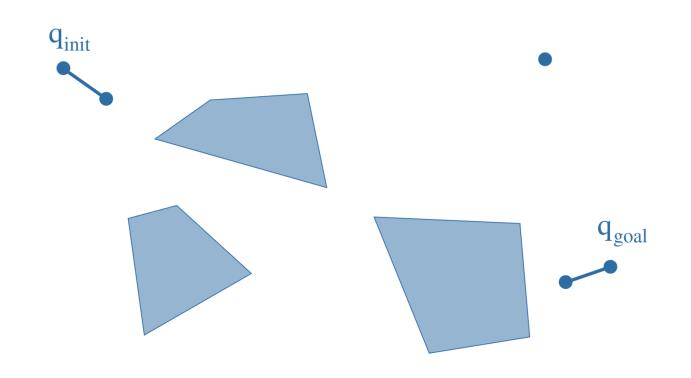


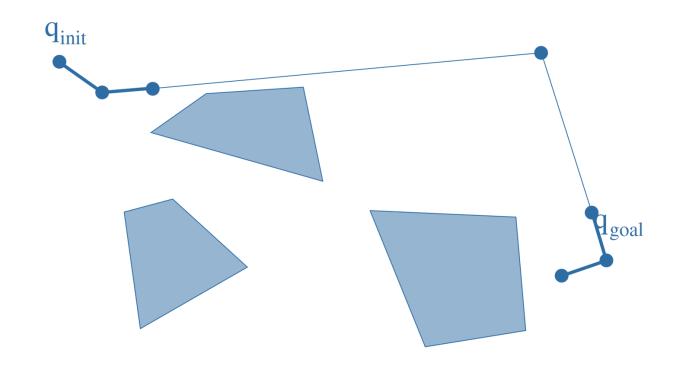


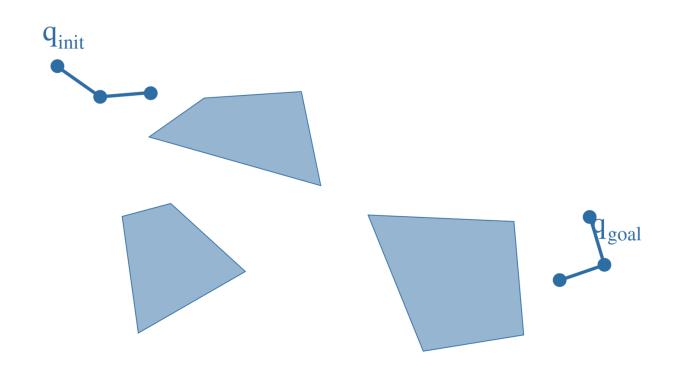


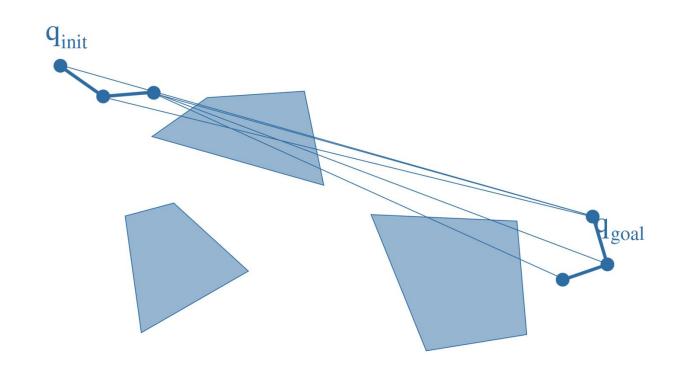


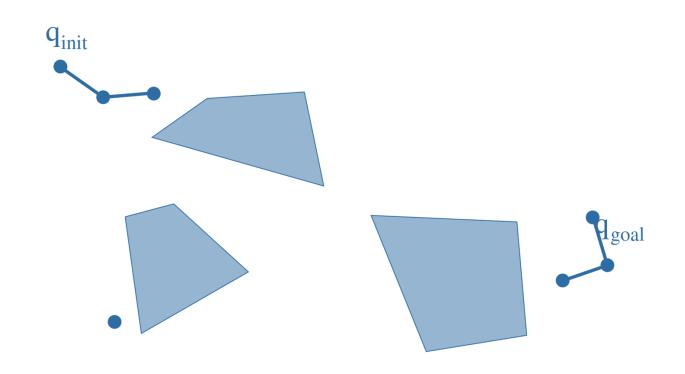


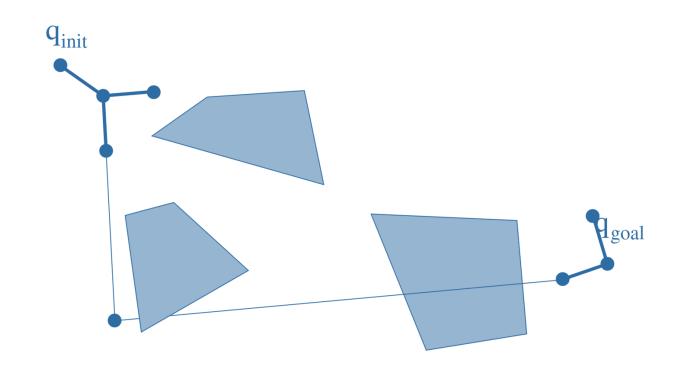


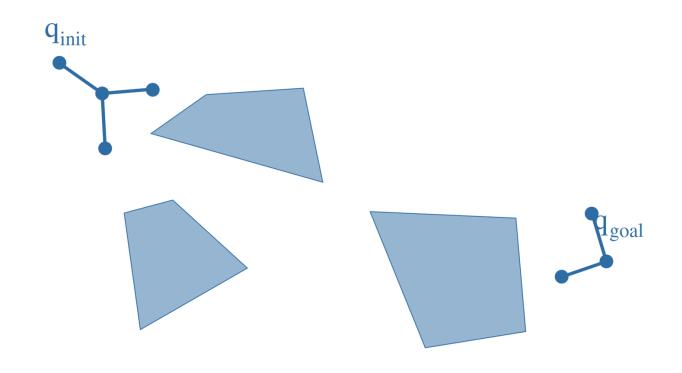


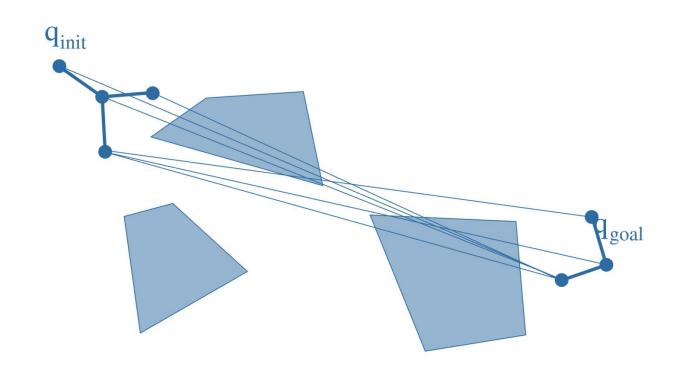


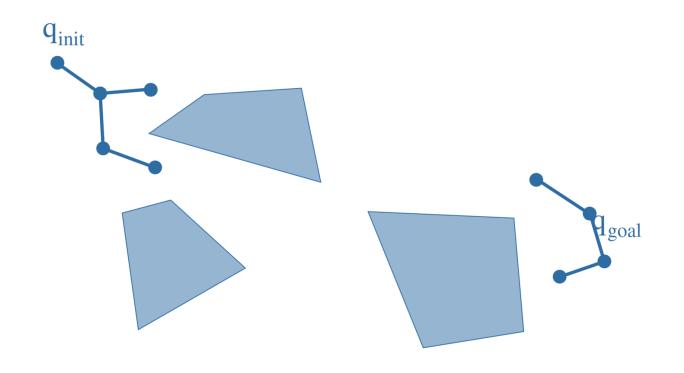


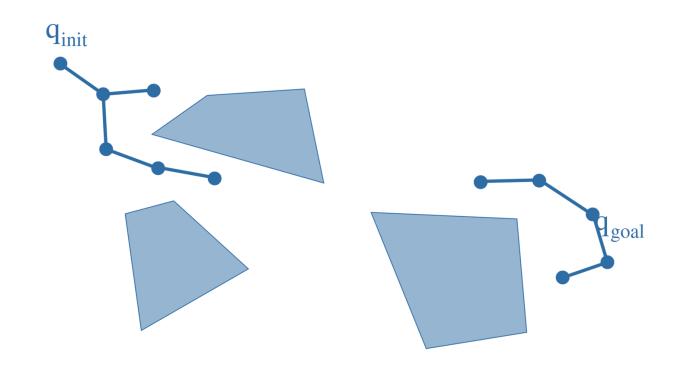


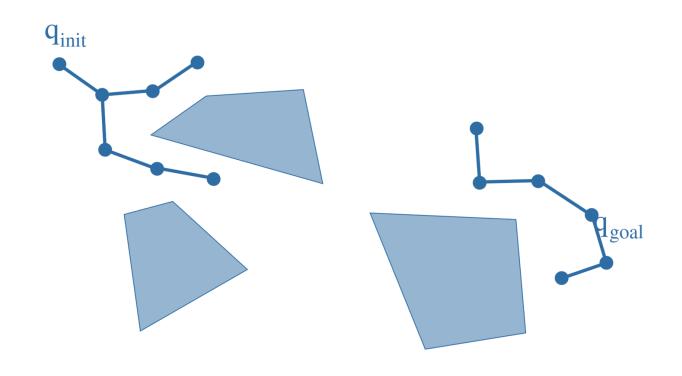


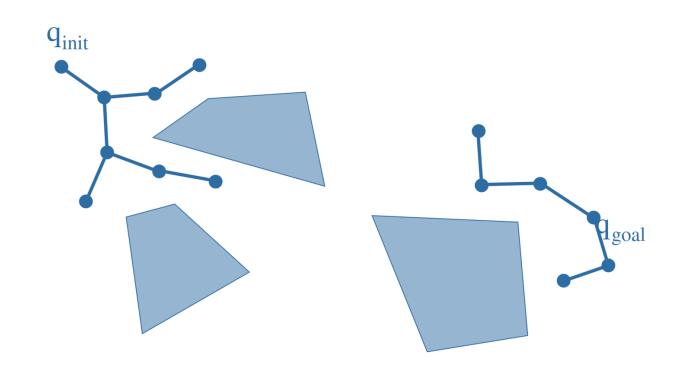


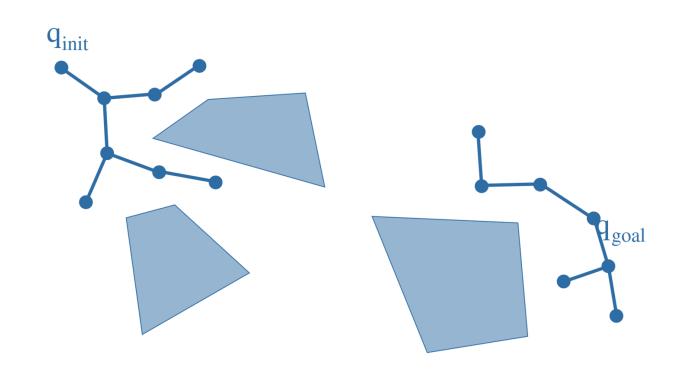


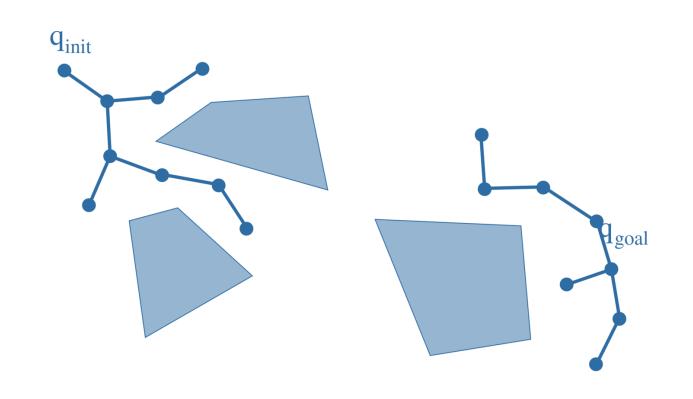


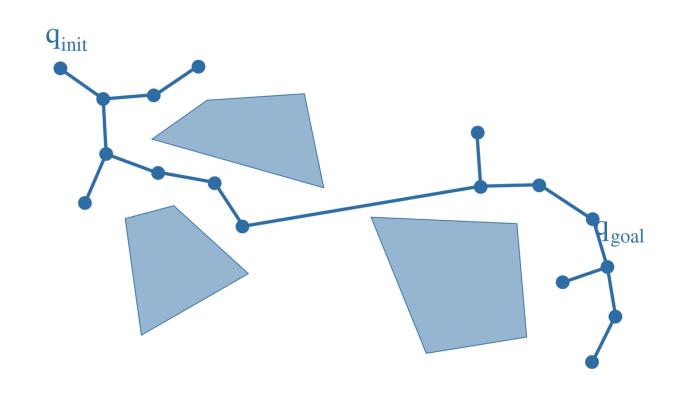


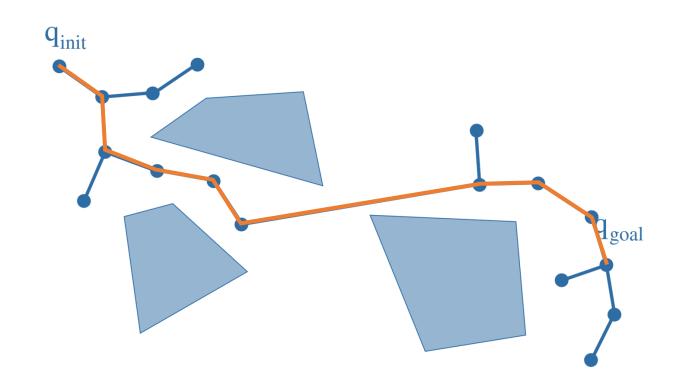












Correctness and complexity

Complexity

- The piano mover problem is PSPACE-hard (Reif, 1979)
- Complexxity of the cylindrical cell decomposion: running time bounded by $(md)^{O(1)^n}\,m$ number of Polynoms, d maximum degree of polynoms, n dimension of the C-space
- Canny's algorithm : $m^n(\log(d))^{O(n^4)}$

Correctness

Completeness

 The algorithm can find in finite time a solution or report in finite time the absence of solution

Resolution completeness

- If the sampling is deterministic following a dense sequence, then the algorithm will find in finite time a solution if it exists
- The algorithm cannot report in finite time the absence of solution

Probablistic completeness

- If a solution exists, then the probability of the algorithm of find the solution tends to 1 as the number of samples/expansions tend to infinity
- The algorithm cannot report in finite time the absence of solution

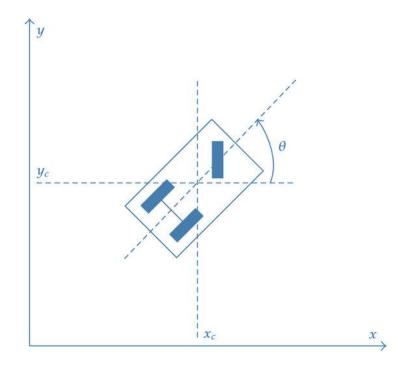
Correctness

- Exact roadmap building and cell decomposition methods are complete (certical cell decomposition, cylindrical cell decomposition)
- Sampling-based methods (PRM, RRT)
 - are probabilistically complete if random sampling is used
 - are resolution complete if a deterministic dense sampling sequence is used

Path/motion planning for non holonomic systems

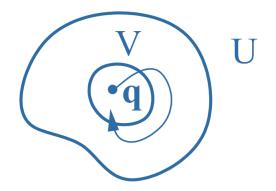
Nonholonomic systems

- Nonholonomic systems involve differential constraints
- e.g. a mobile robot (car) only has two kinematic controls
 - steering wheel
 - gaz/brake
- but evolves in SE(2) (3-d)
- Notion of admissible paths



Controllability of nonholonomic systems

• Nonhonolonomic systems are locally controllable iff for any q in $\mathcal C$ and any neighborhood U of q there exists a neighborhood V of q completely reachable from q by admissible paths included in U

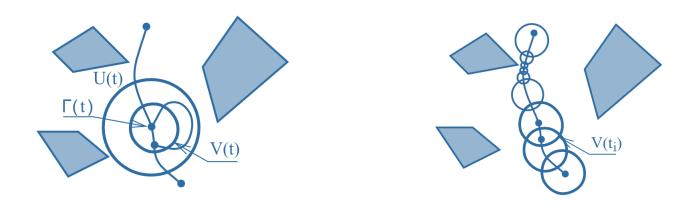


Controllability of nonholonomic systems

- It can be demonstrated that a nonhonolmic system is controllable iff the dimension of the the control vector field Lie Algebra of the system is \boldsymbol{n}
- Lie brackets of control field add the missing dimensions
- E.g. for a mobile robot, or a car, the Lie bracket of the two control vector field correspond to the parallel parking maneuver (créneau) that makes the system move sideways (which was the missing dimension in the control)

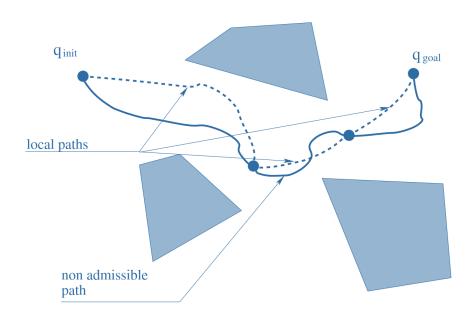
Reduction property

• For a locally controllable system, the existence of a collision-free path between two points of the uncontrained system in SE(2) is equivalent to the existence of a collision free adimissible path for the constrained nonholonomic system



Path planning for nonholonomic systems

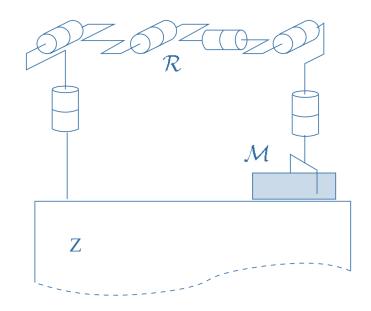
 Path planning for nonholonomic systems is based on path planning of unconstrained system and deformation by dichotomy of non admisible paths applying a local steering method



Manipulation planning

Manipulation planning

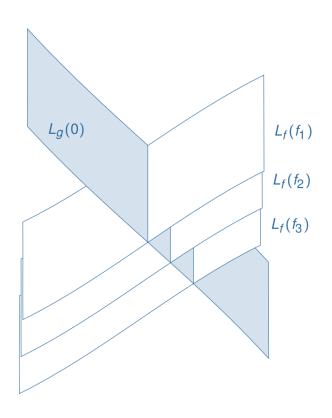
- Motion planning in SE(3) for a manipulated object $\mathcal M$ that cannot "move on its own"
- Can only move indirectly through interaction with robot $\mathcal R$ or lie at rest on environment $\mathcal Z$



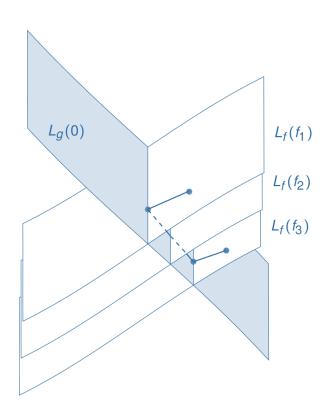
Stratification and foliation of the configuration space

- The configuration space $\mathcal{C} = \mathcal{C}_{\mathcal{R}} \times \mathcal{C}_{\mathcal{M}}$ is stratified in two strata:
 - Set of configurations in which the robot is grasping the object
 - Set of configurations in which the object is lying at rest
- Each stratum is foliated
 - the foliation of the grasp stratum is induced by the relative position of the robot and the grasp (infinitely many)
 - the foliation of rest stratum is induced by the position at which the object rest (infinitely many)
- The system can only move through a given leaf of a foliation, it cannot freely move across foliation of the same stratum
- The only way to move from one leaf to another in the same stratum is by going through a connecting leaf on the other stratum (respectively called transit paths and transfer paths)

Manipulation planning



Manipulation planning



Reduction property 2

- If we consider the intersection of the two strata endowed with both foliations (called the bottom stratum), then we can demonstrate that the existence of an admissible manipulation path between two configurations, that is, a finite sequence of transit and transfer paths, reduces to the existence a collision free path that ignores the foliation.
- Same kind of reasoning as for the nonholonomic system

Enter Humanoids (finally)

A path planning or a motion planning problem?

- Both problems are interesting on their own
- The frontier between the two notions was already "blurred" in the case of a mobile robot on the 2D plane: typically your vacuum cleaner robot
- Depends on the scale and level of the problem
- A humanoid wanting to go from point A to point B on Google map is an instance of a pure path planning problem
- At a finer grain a humanoid wanting to move its foot to do one step along the long Google maps path is an instance of a pure motion planning problem
- There are instances that lie between the two levels, we call them multicontact motion planning problems

Definition of a humanoid robot

• $SE(3) \times \mathbb{R}^n$.

Definition of a humanoid robot

- That's a lot of dimensions to play with
 - (6 + 6) legs + (7+7) arm + 2 torso + 2 neck + 6 of SE(3)
 - Up to 46-d, without even accounting for dexterous fingers
- Stratified by each type of contact configuration on the space / Foliated in each stratification
- And on top of that: The balance constraint which is a huge issue
 - probability of any random configuration or any random motion to make a manipulator arm or wheeled robot or multi-legged robot "fall down": 0
 - probability of any random configuration or any random motion to make a bipedal humanoid robot fall down: 1
 - A humanoid is a inherently unstable system, it is an inverted pendulum always on its unstable equilibrium

Approaches to studying humanoids and make them move

- Decoupling: upper body for manipulation / lower body for locomotion and navigation; global planner / local planner
- Interleaving: motion planning and motion control
- Lower body controllers
 - aka walking controllers
 - Based on the physics of inverted pendulums (aka Zero Moment Point (ZMP) or Center of Pressure (COP) control, Capture point control) Kajita et al 2003
 - used on Honda's Asimo
 - "Stabilizers" are lower level control loop that take in charge balance one or two feet
 - We can usually perform path-planning with these controllers
- Upper-body controllers
 - Don't care about balance, leave it to the stabilizer
 - See robot as fancy dual arm manipulator (Pepper-like robot)

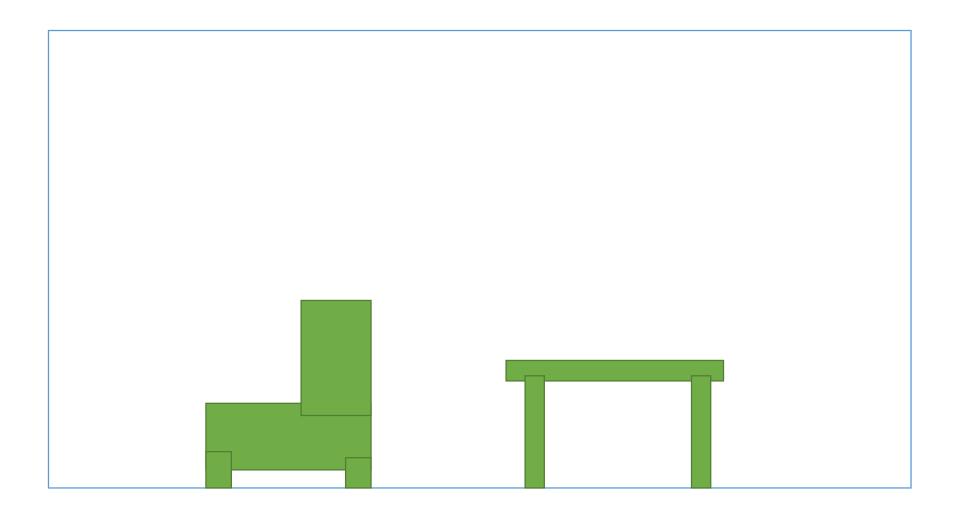
Approaches to studying humanoids and make them move

- Our approach: multi-contact planning and whole-body control
 - See the robot as whole
 - Can use hands for crawling (marcher à 4 pattes), for climbing ladders, stairscases, for walking on hands (why not), can use legs for manipulation (pushing object lying on the floor, kicking a ball)
 - It's just a robot that leaves in its 46-d C-space and happens to have a humanoid shape, no functional decoupling
 - Our philosophy: walking should "emerge" naturally from this approach, not be hard-encoded as a separate control
- Of course, only an ideal objective, as of now, we still encode domainknowledge based heuristics to prune search trees (such as "prefer feet on ground", "prefer hands on table", etc)

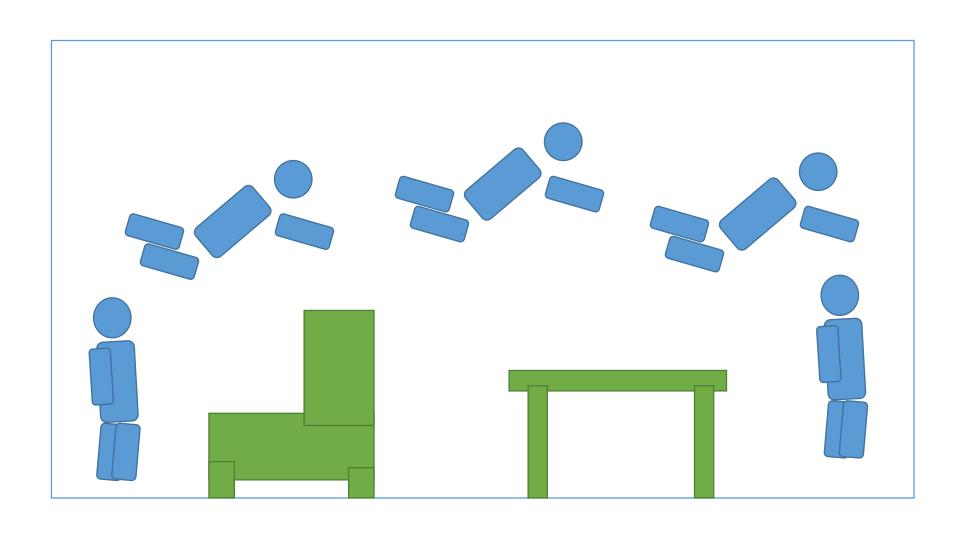
Humanoid multi-contact planning

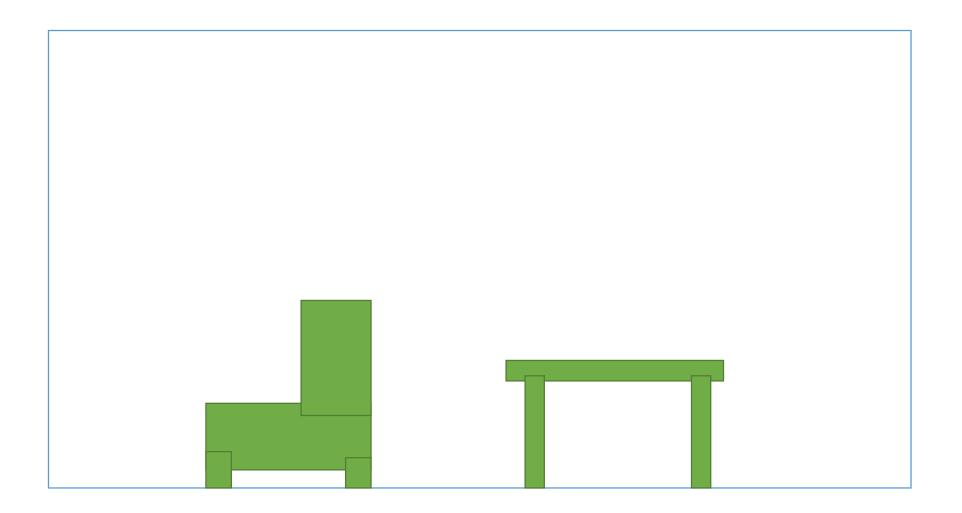
A multi-contact planning instance



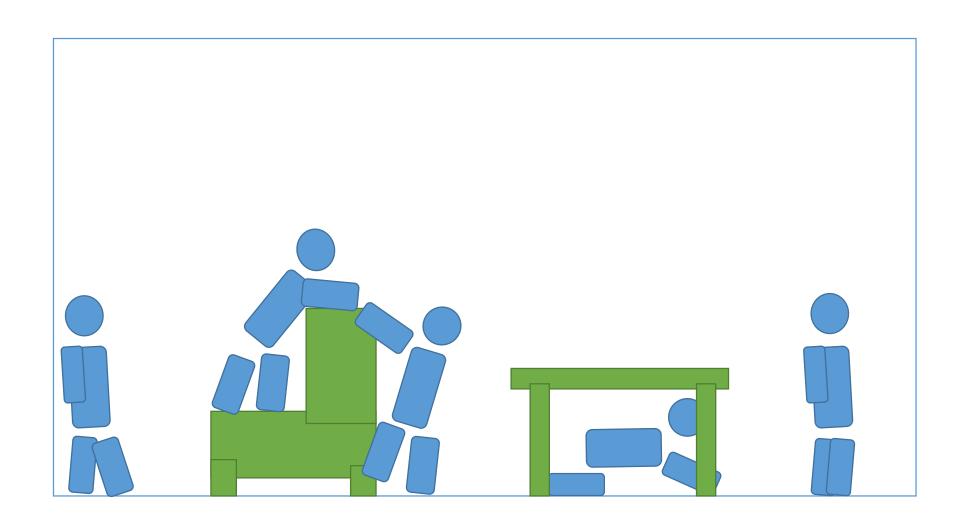


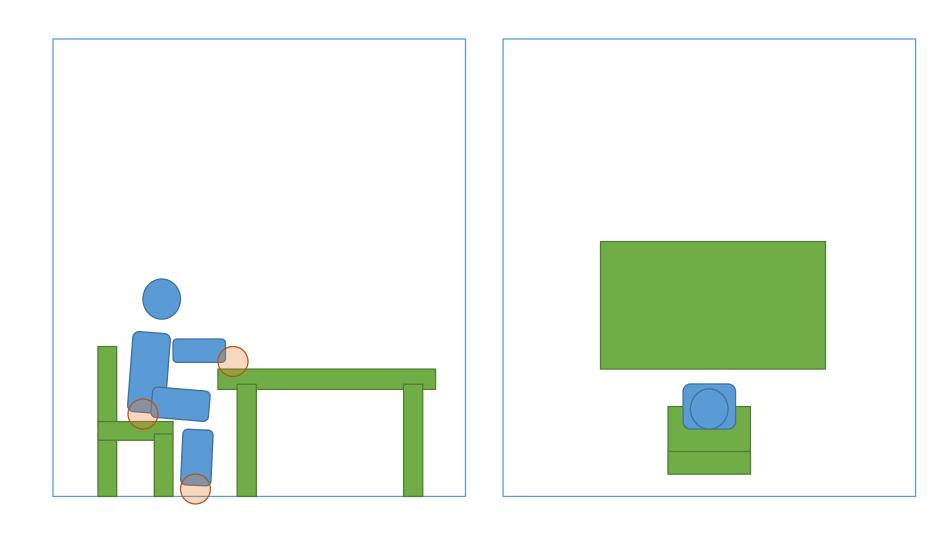
Collision-free path planning/motion planning

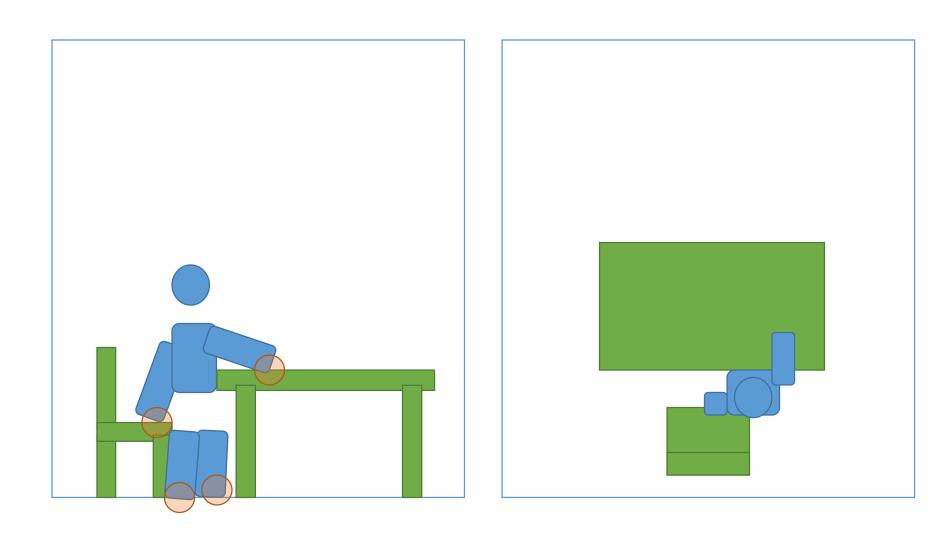


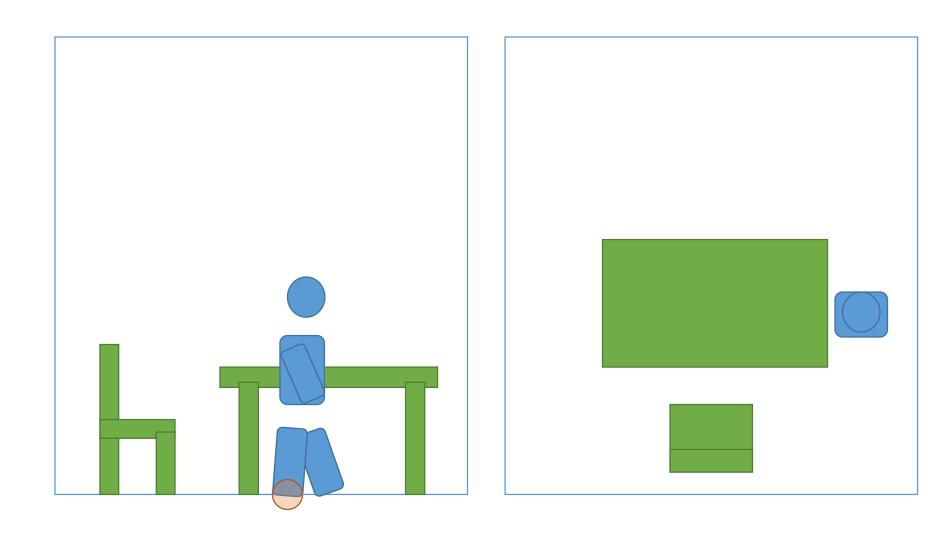


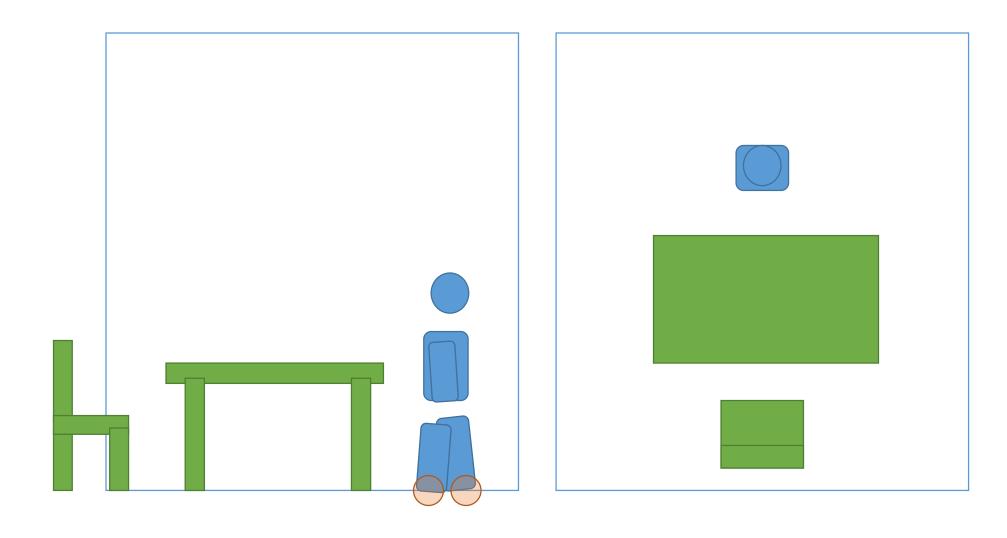
Multi-contact planning











Humanoid multi-contact planning

- Induces the same stratification / foliation structure as the manipulation planning problem
- Each leaf of a stratum corresponds to a stance σ
- a stance σ is a set of contacts
- a contact c is defined as an element of $E = \mathbb{N}^4 \times SE(2)$
- the set of all stances is denoted $\Sigma \subset 2^E$
- Two stances σ and σ' are adjacent if they differ by exactly one contact $\exists c \in E \ \sigma = \sigma' \cup \{c\} \ \text{or} \ \sigma' = \sigma \cup \{c\}$

Humanoid multi-contact planning

- each configuration of the robot q is mapped to a unique stance σ through a forward kinematics function $\sigma = \gamma(q)$
- conversely with each sigma is associated a submanifold of the C-space $Q_{\sigma} = \gamma^{-1}(\{\sigma\})$
- We are interested in a subset $\mathcal{F}_{\sigma} \subset \mathcal{Q}_{\sigma}$ made of physically admissible configurations (existence of admissible contact forces at the contacts of the stance)
- An admissible sequence of stances ("path" in Σ) is a sequence $(\sigma_i)_{i\in\{1,\dots,k\}}$ such that $\forall i\in\{1,\dots,k-1\}$ σ_i is adjacent to σ_{i+1} and $\mathcal{F}_{\sigma_i}\cap\mathcal{F}_{\sigma_{i+1}}\neq\emptyset$

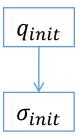
Humanoid motion planning and control framework

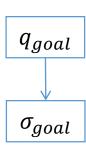
Locomotion query: q_{init} , q_{goal}

 q_{init}

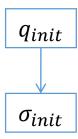
 q_{goal}

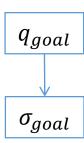
Locomotion query: q_{init} , q_{goal}



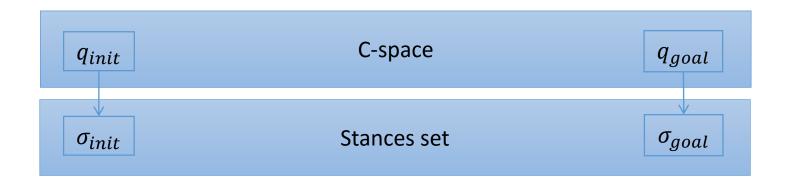


Locomotion query: q_{init} , q_{goal}

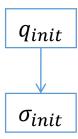


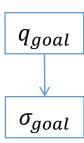


Locomotion query: q_{init} , q_{goal}

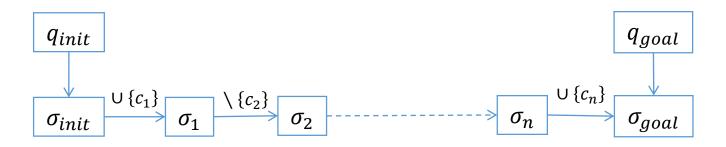


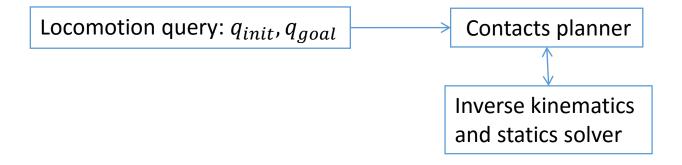
Locomotion query: q_{init} , q_{goal}

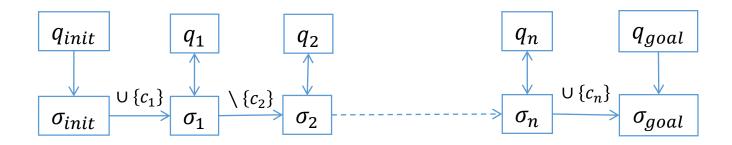


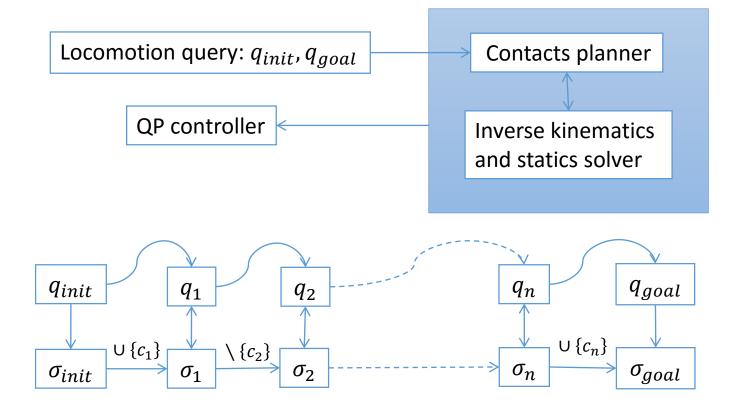


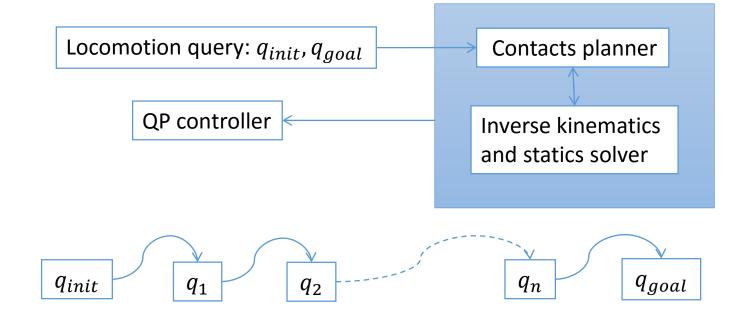
Locomotion query: q_{init} , q_{goal} Contacts planner

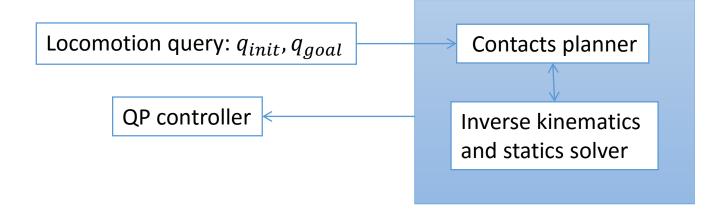


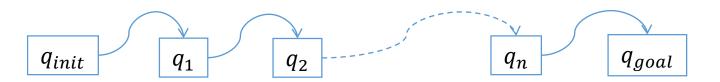


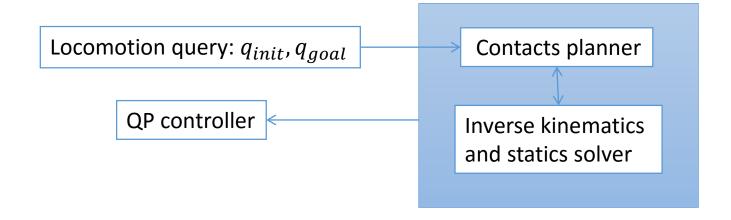


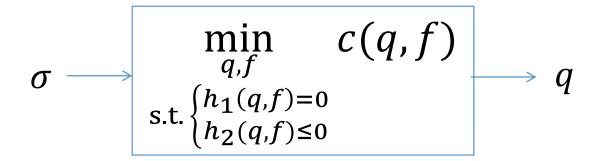




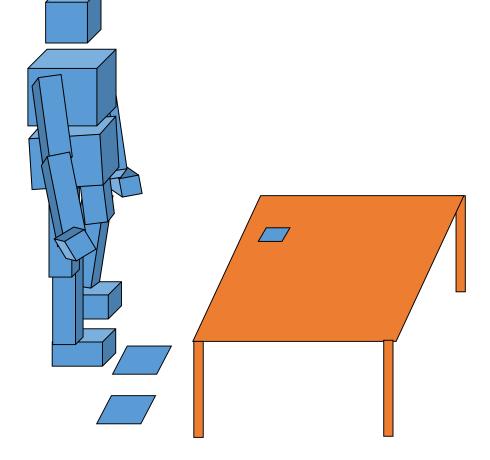


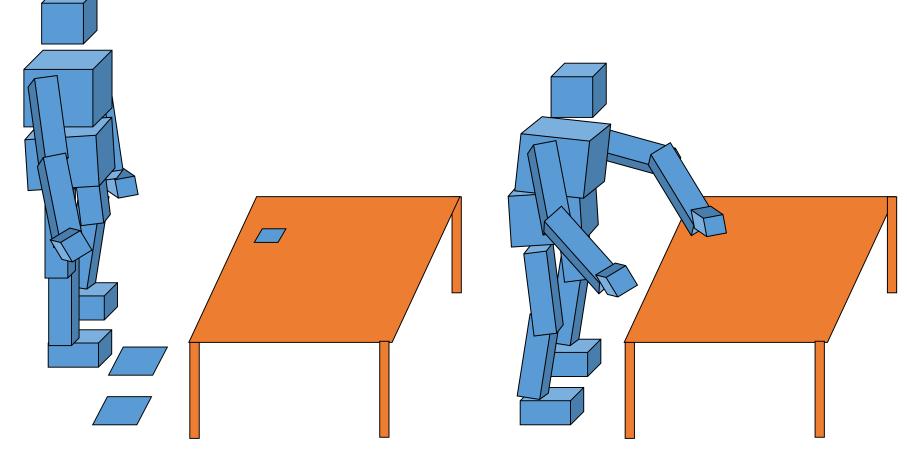


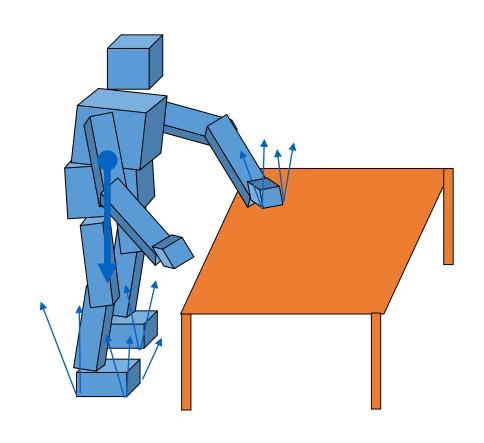


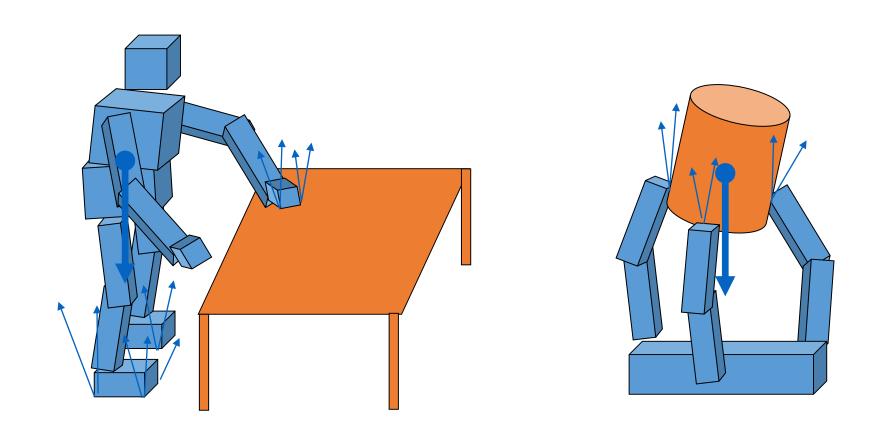


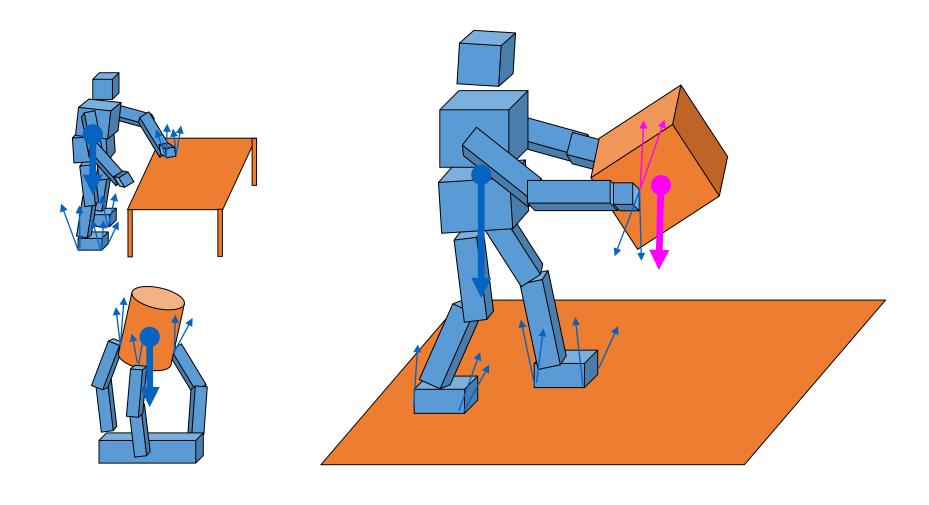
- c(q, f) distance of q to a reference nominal posture q_{ref} + norm of f
- $h_1(q, f) = 0$ fixed contacts positions, static equilibrium equation (free-flyer part)
- $h_2(q, f) \le 0$ floating contacts positions, joint limits, static equilibrium equation (actuated part, torque limits), friction cones, collision-avoidance

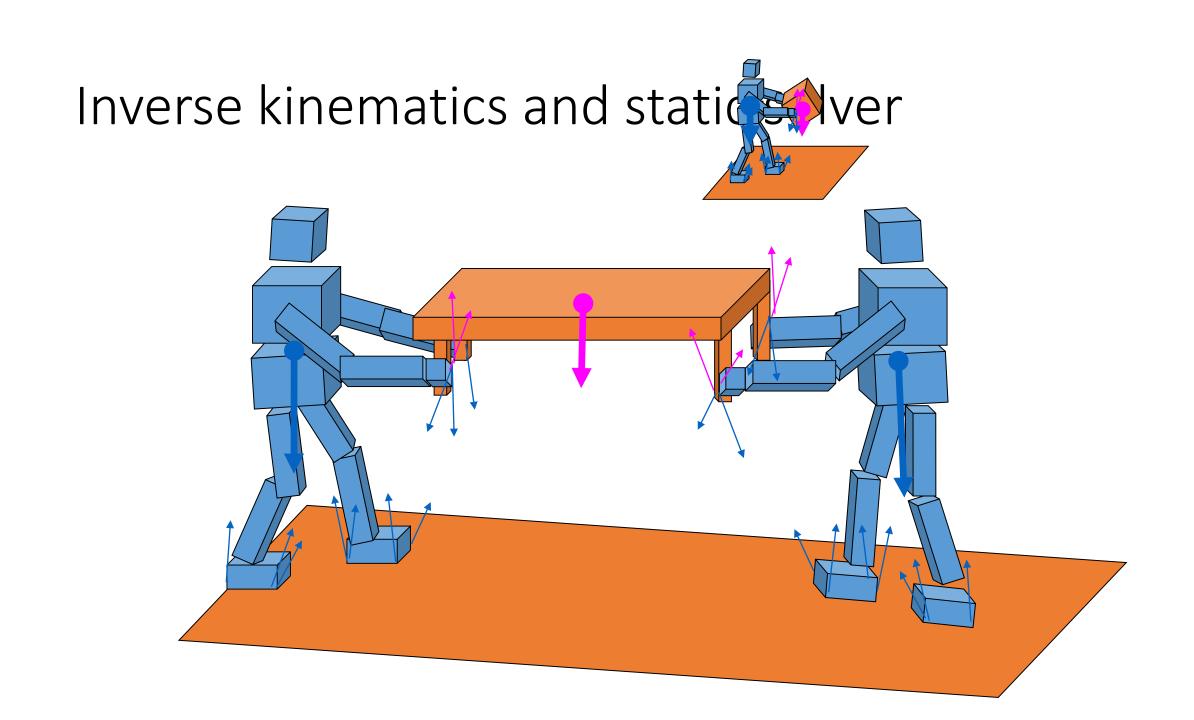






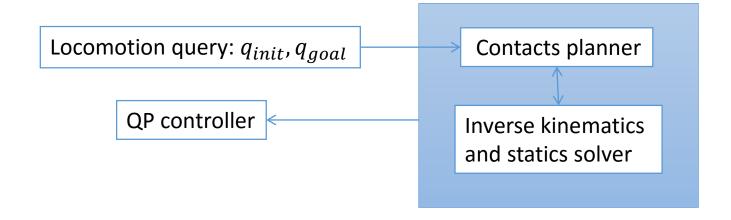






Locomotion-and-Manipulation Manipulation Locomotion

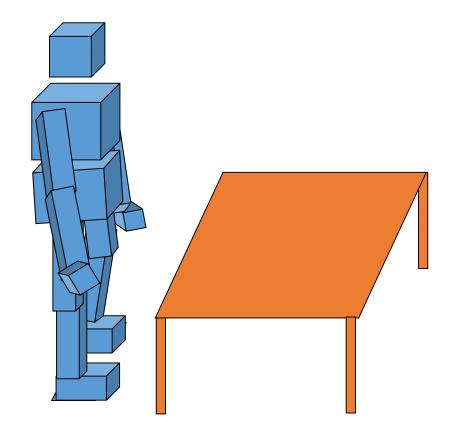


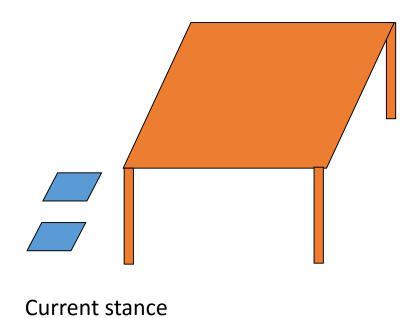


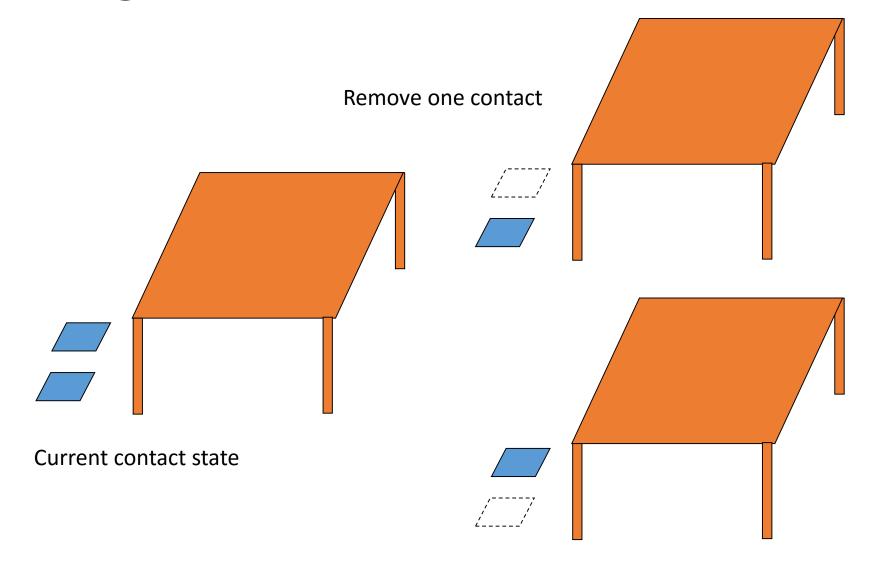
Contacts planner

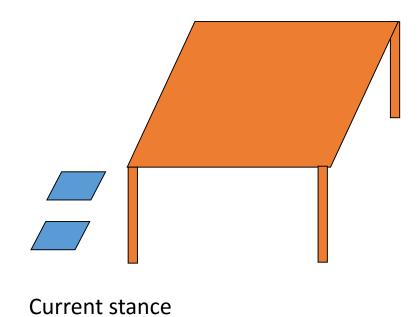
Best-First Search

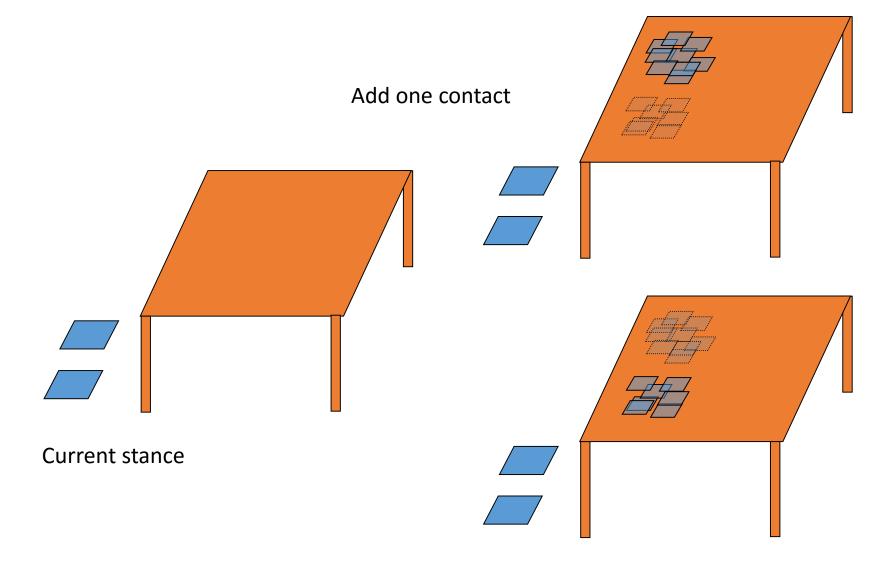
- Initialize a search tree and a priority queue with the initial stance
- Loop:
 - Pop most promising stance from the priority queue
 - For all present contacts in this stance
 - Try to remove the contact and see if the robot keeps balance (call the IKS)
 - If so, push the new stance into the priority queue and add it as a leaf in the tree
 - For all unused bodies in this stance
 - Try to add the unused body to the stance and see if the robot can reach balance (call the IKS)
 - If so, push the new stance into the priority queue and add it as a leaf in the tree
- Until reaching the goal

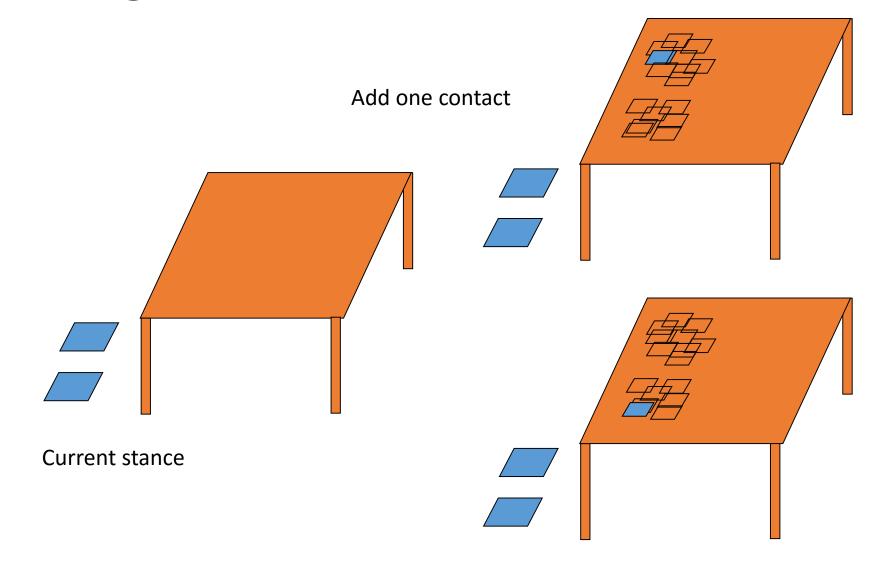


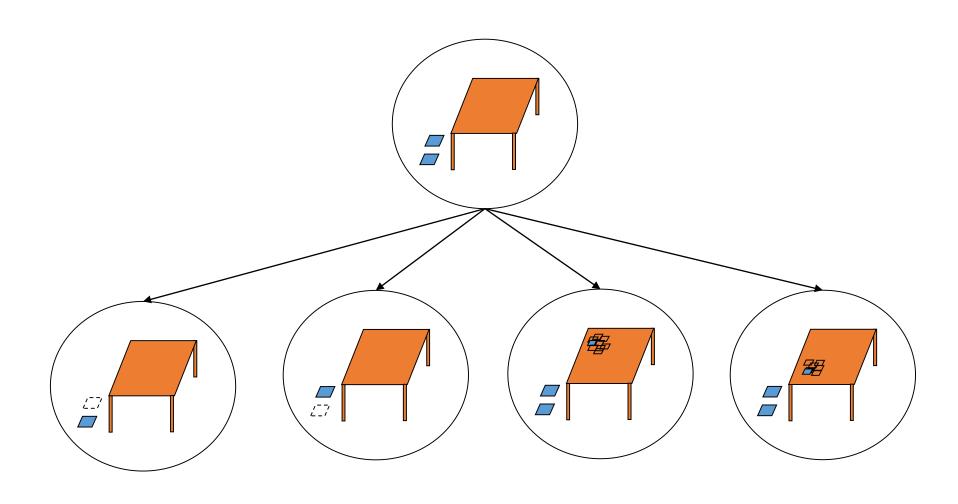


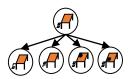


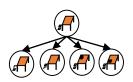


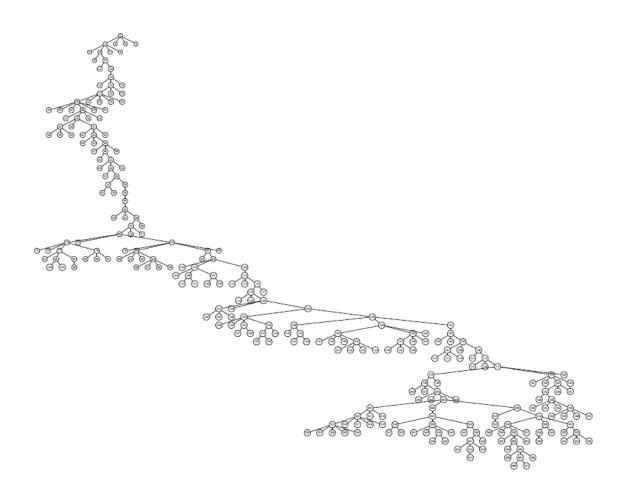




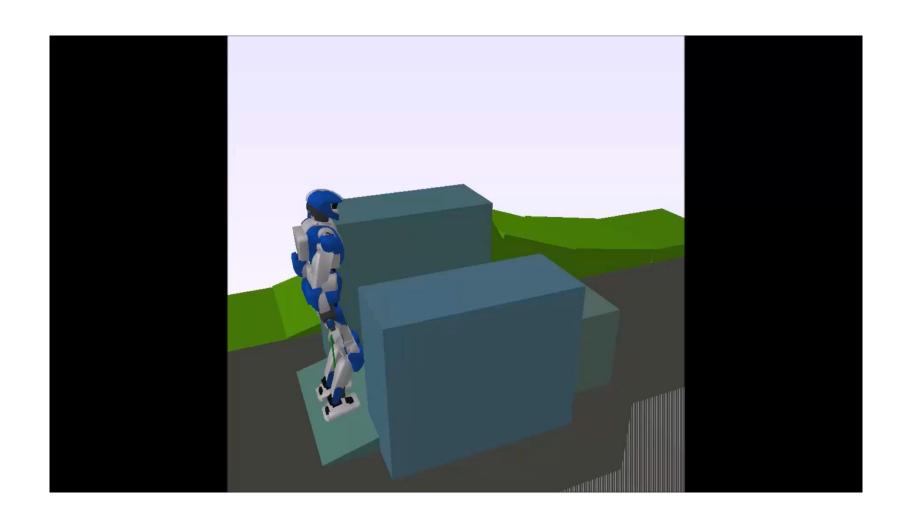




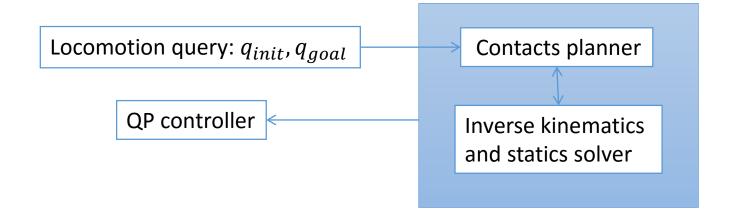




Search algorithm



Overview of the Framework



Overview of the Framework

QP controller

Basic idea: at a given q, \dot{q} , the dynamics equation of motion is linear in \ddot{q} , τ , f:

$$M(q)\ddot{q} + N(q,\dot{q}) = S\tau + J^T f$$

$$\min_{\substack{\ddot{q},f,\tau\\ \ddot{q},f,\tau\\ J\ddot{q}+N(q,\dot{q})=S\tau+J^Tf\\ J\ddot{q}+\dot{J}\dot{q}=0\\ Kf\geq 0\\ |\tau|\leq \tau_{max}}} \sum_{k} w_k \left\| \ddot{g}_k - \ddot{g}_k^{\ d} \right\|^2$$

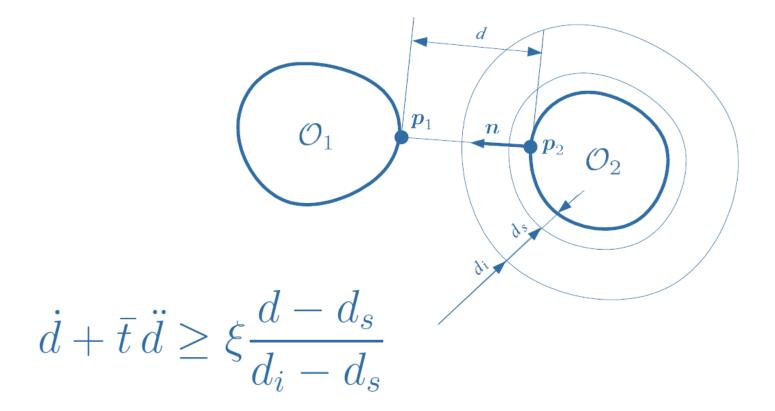
$$\min_{\substack{\ddot{q},f,\tau\\ \ddot{q},f,\tau\\ J\ddot{q}+\ddot{J}\dot{q}=0\\ Kf\geq 0\\ |\tau|\leq \tau_{max}}} \sum_{k} w_{k} \|\ddot{g}_{k}-\ddot{g}_{k}^{d}\|^{2} \longrightarrow \ddot{q}$$

$$\min_{\substack{\ddot{q},f,\tau\\ \ddot{q},f,\tau\\ J\ddot{q}+\ddot{J}\dot{q}=0\\ Kf\geq 0\\ |\tau|\leq \tau_{max}}} \sum_{k} w_{k} \|\ddot{g}_{k}-\ddot{g}_{k}^{d}\|^{2} \longrightarrow \ddot{q} \stackrel{\int}{\longrightarrow} \dot{q} \stackrel{\int}{\longrightarrow} q$$
• Position control • Simulation

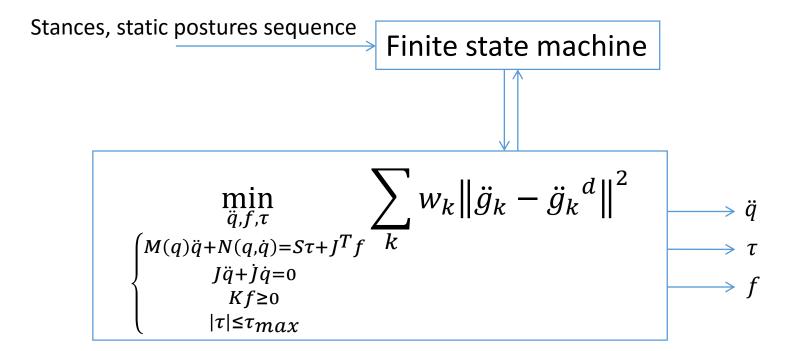
$$\min_{\substack{\ddot{q},f,\tau\\ \ddot{q},f,\tau\\ J\ddot{q}+\ddot{J}\dot{q}=0\\ Kf\geq 0\\ |\tau|\leq \tau_{max}}} \sum_{k} w_{k} \|\ddot{g}_{k}-\ddot{g}_{k}^{d}\|^{2}$$

$$\uparrow$$
Torque command
• to real robot
• to physics simulator

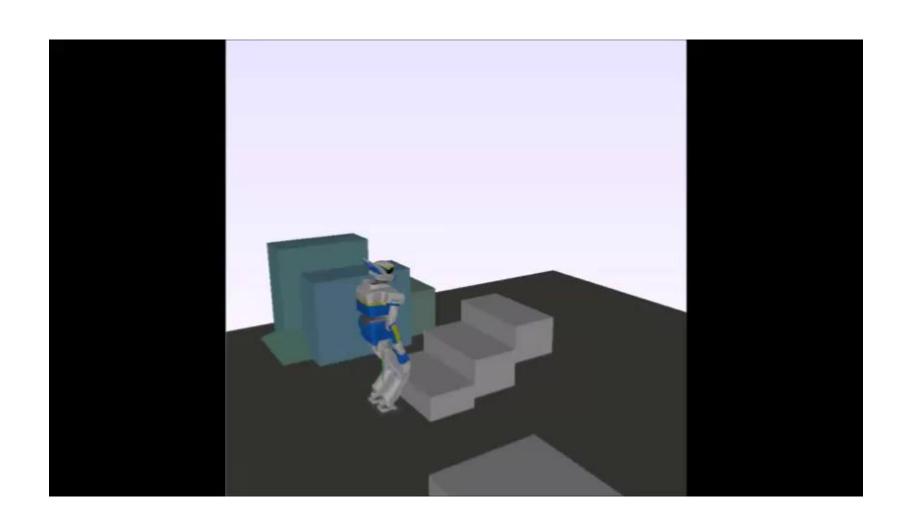
 Online collision avoidance linear constraint based on velocity-damper formulation (Kanehiro et al, RSS 2008)



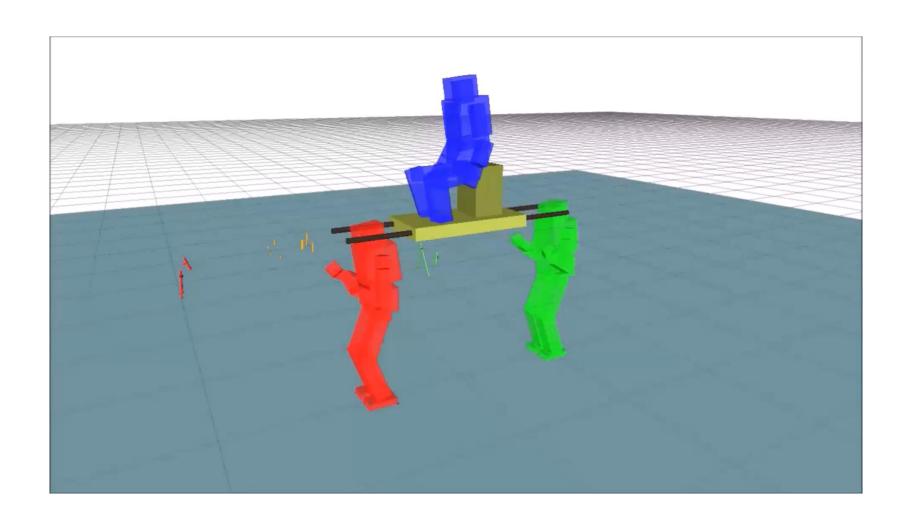
$$\min_{\substack{\ddot{q},f,\tau\\ \ddot{q},f,\tau\\ J\ddot{q}+\ddot{J}\dot{q}=0\\ Kf\geq 0\\ |\tau|\leq \tau_{max}}} \sum_{k} w_{k} \|\ddot{g}_{k}-\ddot{g}_{k}^{d}\|^{2} \longrightarrow \ddot{q}$$



- QP control has become golden standard in humanoid robotics
 - All DARPA Robotics Challenge teams used a version of QP control on their robots







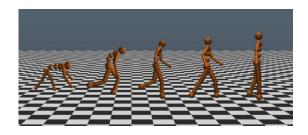
What's next

Many topics we didn't cover

- Perception
 - Humanoid mult-contact visual SLAM (Simultaneous Localization and Mapping)
- Stability of the control
- Robustness to modelling uncertainties
- Middleware control architectures
- Hardware

What's next in humanoid motion planning and control?

- Exciting new software developments, leveraging ML techniques, deep RL techniques, and evolutionary algorithms
 - Google Deepmind "Emergence of Locomotion Behaviours in Rich Environments"
 - Uber AI labs "Welcoming the Era of Deep Neuroevolution"

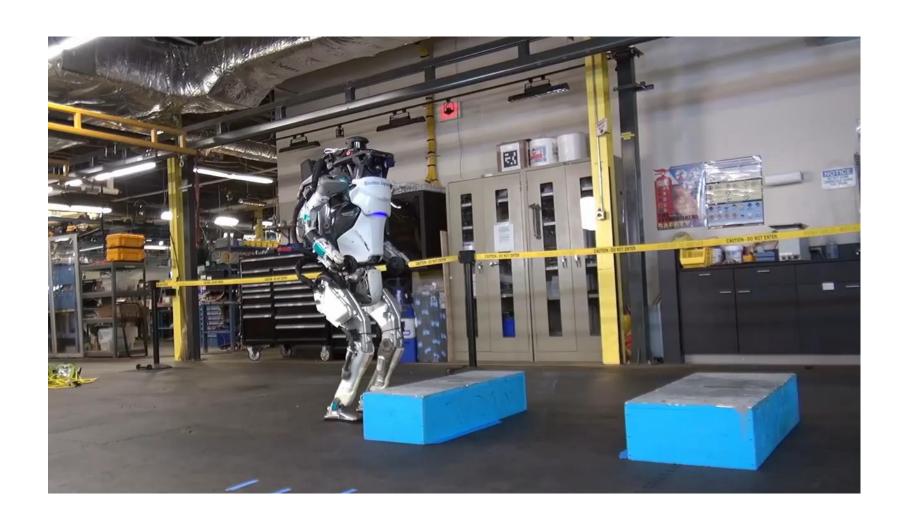


- We are currently working in our team on applying trial and error learning techniques based on evolutionary CMA-ES optimization in multi-contact QP control (Spitz et al, Humanoids 2017)
- Exciting new hardware developments
 - Hardware has always been a big limitation
 - Boston Dynamics' backflip!
 - New hardware paradigms based on series elastic actuators, artificial muscles, highly resilient hardware capable of sustaining more extreme motion
 - Highly dynamic motions ahead

Deep Reinforcement Learning



Super hardware



Thank you for your attention