

# Master 2 Mathematics and Computer Science

## Symbolic Dynamics. Quizz

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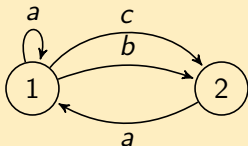
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## Quizz

## Exercise 1

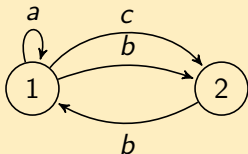
Is the shift space of labels of bi-infinite paths of the following automaton



- a sofic shift?
- an irreducible sofic shift?
- a shift of finite-type?
- a shift conjugate to an edge shift? If yes, exhibit a conjugacy.

## Exercise 2

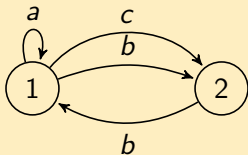
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## Exercise 3

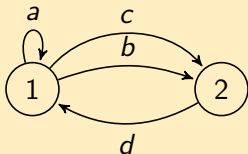
Compute the entropy of the shift space of labels of bi-infinite paths of the following automaton



## Exercise 4

Compute the entropy of the shift space of labels of bi-infinite paths of the following automaton.

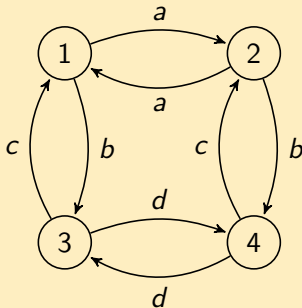
Compute its zeta function.



# Quizz on sofic shifts

## Exercise 5

Is the shift space of labels of bi-infinite paths of the following automaton



- a sofic shift?
- an irreducible sofic shift?
- a shift of finite-type?

## Exercise 6

Let  $X = X_F$  be the shift space on  $A = \{a, b\}$  where  $F = \{aaa\}$ .

- Is  $X$  a shift of finite-type?
- Is  $X$  an irreducible shift of finite type?
- compute a local automaton presenting  $X$ .



## Exercise 7

Let  $\sigma: \{a, b, c\}^* \rightarrow \{a, b, c\}^*$  be the substitution defined by  $a \mapsto bac, b \mapsto bb, c \mapsto cc$ .

- Is this substitution primitive?
- Is this substitution growing?
- Describe  $X(\sigma)$ . What are the points in  $X(\sigma)$ ?
- Is  $X(\sigma)$  a minimal shift space?

## Exercise 8

Let  $\sigma: \{0, 1, 2\}^* \rightarrow \{0, 1, 2\}^*$  be the substitution defined by  $0 \mapsto 0012, 1 \mapsto 12, 2 \mapsto 012$ .

- Is this substitution primitive?
- Is this substitution growing?
- Is  $X(\sigma)$  a minimal shift space?
- Is the block complexity  $p_{X(\sigma)}(n) = \Theta(n)$ ?